


First Observation of CP Violation and Measurement of Polarization in $B^+ \rightarrow \rho(770)^0 K^*(892)^+$ Decays

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An amplitude analysis of the $B^+ \rightarrow (\pi^+\pi^-)(K_S^0\pi^+)$ decay is performed in the mass regions $0.30 < m_{\pi^+\pi^-} < 1.10$ GeV/ c^2 and $0.75 < m_{K_S^0\pi^+} < 1.20$ GeV/ c^2 , using pp collision data recorded with the LHCb detector corresponding to an integrated luminosity of 9 fb⁻¹. The polarization fractions and CP asymmetries for $B^+ \rightarrow \rho(770)^0 K^*(892)^+$ decays are measured. Violation of the CP symmetry in the decay $B^+ \rightarrow \rho(770)^0 K^*(892)^+$ is observed for the first time, with a significance exceeding 9 standard deviations. The CP asymmetry is measured to be $\mathcal{A}_{CP} = 0.507 \pm 0.062(\text{stat}) \pm 0.024(\text{syst})$ and the CP -averaged longitudinal polarization fraction of $f_L = 0.720 \pm 0.028(\text{stat}) \pm 0.009(\text{syst})$. The measurements help to shed light on the polarization puzzle of B mesons decaying to two vector mesons.

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Decays of beauty mesons provide a rich phenomenology to study the standard model (SM) of particle physics and investigate potential new physics effects. Charmless B -meson decays into two vector mesons (V), $B \rightarrow VV$, serve as a powerful probe for the dynamics of weak and strong interactions through their angular distributions. Since $B \rightarrow VV$ decays generally proceed through transitions at both leading-order (tree-level) and higher-order (loop), they carry information about the SM flavor structure and the Cabibbo-Kobayashi-Maskawa matrix [1]. The interference between the loop and tree-level processes gives rise to the combined charge conjugation and parity (CP) violation, a phenomenon required to explain the matter-antimatter asymmetry of the Universe.

Every $B \rightarrow VV$ decay receives contributions from three helicity amplitudes, which, with an appropriate choice of basis, can be described by longitudinal (A_0), perpendicular (A_\perp), and parallel (A_\parallel) components encoding different orbital angular momentum configurations between the two vector mesons [2], allowing to study the spin structure of the flavor-changing interaction. These amplitudes can be distinguished by studying the angular distributions of the decay products of the two vector mesons, enabling measurements of the weak and strong phases, as well as the longitudinal polarization fraction $f_L \equiv |A_0|^2 / (|A_0|^2 + |A_\perp|^2 + |A_\parallel|^2)$. While the SM predicts an almost total longitudinal polarization, $f_L \approx 1$,

by a naive factorization ansatz [3], f_L is measured to span the range from around 10% to almost 100% across different $B \rightarrow VV$ decay modes [4–17]. Explanations proposed to resolve this “polarization puzzle” include enhanced contributions from weak-annihilation amplitudes [18–22], charm-loop diagrams [23,24], higher-order corrections [25,26], final-state interactions [27–30], as well as physics beyond the SM [31–36]. These contributions may also have a significant impact on predictions of CP asymmetries in $B \rightarrow VV$ decays [26]. To date, a coherent description of CP violation and polarization in $B \rightarrow VV$ decays remains challenging.

The specific class of $B \rightarrow VV$ decays with $B \rightarrow \rho K^*$ has been widely studied, where, throughout this Letter, ρ and K^* represent the $\rho(770)$ and $K^*(892)$ mesons, respectively, unless otherwise stated. The longitudinal fractions are measured to be substantially different depending on the final state, with $f_L(B^+ \rightarrow \rho^0 K^{*+}) = 0.78 \pm 0.12$ [37], $f_L(B^+ \rightarrow \rho^+ K^{*0}) = 0.48 \pm 0.08$ [5,38,39], $f_L(B^0 \rightarrow \rho^0 K^{*0}) = 0.173 \pm 0.026$ [15,38,40], and $f_L(B^0 \rightarrow \rho^- K^{*+}) = 0.38 \pm 0.13$ [40], where charge conjugation is implied throughout this Letter unless otherwise specifically stated. These observed discrepancies reflect the varying interference patterns between tree-level and loop processes [41], which would also be revealed by measuring the CP asymmetries. Among these decays, CP violation has only been established in the longitudinal component of the $B^0 \rightarrow \rho^0 K^{*0}$ decay [15]. Detailed and precise measurements of $B \rightarrow \rho K^*$ decays, compared with various predictions [2,20–22,24,25,41–46], permit more precise extractions of nonperturbative parameters through global fits [46] and help to shed light on the polarization puzzle and the dynamics of CP violation in these decays. They also comprise fundamental input for theoretically clean,

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model-independent isospin sum rules that are highly sensitive to physics beyond the SM [47].

In this Letter the measurements of polarization and CP parameters in the $B^+ \rightarrow \rho^0 K^{*+}$ decay are reported. The reconstruction of the ρ^0 and K^{*+} mesons are performed in the decays $\rho^0 \rightarrow \pi^+ \pi^-$ and $K^{*+} \rightarrow K_S^0 \pi^+$, respectively. An amplitude analysis of the $B^+ \rightarrow (\pi^+ \pi^-)(K_S^0 \pi^+)$ decay is performed, using pp collision data collected with the LHCb detector at center-of-mass energies of $\sqrt{s} = 7, 8$ (Run 1 period in years 2011 and 2012) and 13 TeV (Run 2 period in years 2015–2018), corresponding to a total integrated luminosity of 9 fb^{-1} .

The LHCb detector is a single-arm forward spectrometer dedicated to the study of heavy flavor hadrons and is described in detail in Refs. [48,49]. The online event selection is performed by a trigger [50,51], which consists of a hardware stage followed by a software stage. The hardware trigger selects hadron, muon, electron, and photon candidates with high transverse momentum (p_T) based on information from the calorimeter and muon systems. The software stage, which applies a full event reconstruction, identifies a secondary vertex with a significant displacement from any primary pp interaction vertex (PV) by means of a multivariate algorithm. Simulated $B^+ \rightarrow \rho^0 K^{*+}$ decays are produced with the software described in Refs. [52–59], and are used to model the effects of the detector acceptance, resolution, and selection requirements. The simulation is subjected to the same selection requirements applied to data.

In the off-line analysis, five charged tracks identified as pions are used to build the B^+ candidate according to the decay sequence $B^+ \rightarrow \rho^0 (\rightarrow \pi^+ \pi^-) K^{*+} (\rightarrow K_S^0 \pi^+)$, with $K_S^0 \rightarrow \pi^+ \pi^-$. The pions are required to be inconsistent with being produced from any PV. The K_S^0, ρ^0, K^{*+} , and B^+ candidates are required to have well-reconstructed decay vertices [49] and significant displacement from any PV. The reconstructed K_S^0 mass should be consistent with its known value [38]. The masses of ρ^0 and K^{*+} candidates are required to be within the ranges $0.30 < m_{\pi^+ \pi^-} < 1.10 \text{ GeV}/c^2$ and $0.75 < m_{K_S^0 \pi^+} < 1.20 \text{ GeV}/c^2$, respectively, to contain most of the resonant contributions given their large natural widths. After applying the two mass-window requirements, candidates with the interchange of the two same-charge pions are negligible. Any B^+ candidate with mass in the range $4.90 < m_{\pi^+ \pi^- K_S^0 \pi^+} < 5.80 \text{ GeV}/c^2$ is retained for further analysis.

The $K_S^0 \rightarrow \pi^+ \pi^-$ candidates are contaminated by $\Lambda \rightarrow p \pi^-$ decays, where the proton is misidentified as a pion. This background is reduced to a negligible level by vetoing K_S^0 candidates with mass consistent with the known Λ mass [38], when the energy of a pion is calculated under the proton mass hypothesis. The same approach is applied to suppress decays involving intermediate charmed states. For example, the $B^+ \rightarrow \bar{D}^0 (\rightarrow K_S^0 \pi^+ \pi^-) \pi^+$ decay is

removed by vetoing candidates with $K_S^0 \pi^+ \pi^-$ mass near the known D^0 mass [38].

To further suppress background due to random combinations of final-state tracks, a boosted decision tree (BDT) classifier [60,61] implemented in the TMVA toolkit [62,63] is employed. The variables discriminating signal and background include the geometrical and kinematical properties of the decay. The BDT classifier is trained using simulated $B^+ \rightarrow \rho^0 K^{*+}$ decays as a proxy for the signal and data candidates in the high $\pi^+ \pi^- K_S^0 \pi^+$ mass region, $5.40 < m_{\pi^+ \pi^- K_S^0 \pi^+} < 5.80 \text{ GeV}/c^2$, for the background. The requirement on the BDT response is optimized simultaneously with the particle identification of pions, by maximizing the figure of merit defined as $S/\sqrt{S+B}$. The quantities S and B are the signal and background yields estimated in the signal region chosen as $\pm 0.043 \text{ GeV}/c^2$ around the known B^+ mass of $5.279 \text{ GeV}/c^2$ [38], approximately 2.5 times the experimental mass resolution.

An extended unbinned maximum-likelihood fit is performed simultaneously to the $m_{\pi^+ \pi^- K_S^0 \pi^+}$ and $m_{\pi^- \pi^+ K_S^0 \pi^-}$ distributions in the range $4.90 < m_{\pi^\pm \pi^\mp K_S^0 \pi^\pm} < 5.60 \text{ GeV}/c^2$, as shown in Fig. 1, where the shape parameters for each component are shared for B^+ and B^- decays, with the yields allowed to differ between the two samples. The fit model consists of the combination of a Gaussian function and a Crystal Ball function [64] to describe the signal, and an exponential function for the combinatorial background. An ARGUS function [65] is used to describe partially reconstructed backgrounds, such as the $B^{0,+} \rightarrow (\pi^+ \pi^-)(K_S^0 \pi^+) \pi^{-,0}$ decay where the additional $\pi^{-,0}$ meson is not reconstructed. The numbers of B^+ and B^- signal candidates are determined to be 2208 ± 53 and 2333 ± 55 , respectively, where the uncertainties are statistical. The subsequent amplitude analysis exploits candidates in the signal region, chosen as $5.24 < m_{\pi^\pm \pi^\mp K_S^0 \pi^\pm} < 5.32 \text{ GeV}/c^2$. Within this region, the fraction of B^+ (B^-) combinatorial background over the total signal and background yield of both flavors is $r_b^+ = 0.0631 \pm 0.0032$ ($r_b^- = 0.0633 \pm 0.0032$), where the uncertainties are statistical only. The charge asymmetry is not significant for either the combinatorial background or the signal. The amount of partially reconstructed background in the signal regions is negligible.

An amplitude analysis is performed to study the different contributions to the decay, thereby enabling measurements of the polarization and the CP asymmetry for each component. The kinematics of the $B^+ \rightarrow (\pi^+ \pi^-)(K_S^0 \pi^+)$ decay can be fully described by five independent variables, $\vec{O} = (m_{\pi^+ \pi^-}, m_{K_S^0 \pi^+}, \cos \theta_{\pi^+ \pi^-}, \cos \theta_{K_S^0 \pi^+}, \phi)$, where $m_{\pi^+ \pi^-}$ and $m_{K_S^0 \pi^+}$ are the masses, $\theta_{\pi^+ \pi^-}$ and $\theta_{K_S^0 \pi^+}$ are the helicity angles, and ϕ is the angle between the $\rho^0 \rightarrow \pi^+ \pi^-$ and $K^{*+} \rightarrow K_S^0 \pi^+$ decay planes. The variable $\theta_{\pi^+ \pi^-}$ ($\theta_{K_S^0 \pi^+}$) is

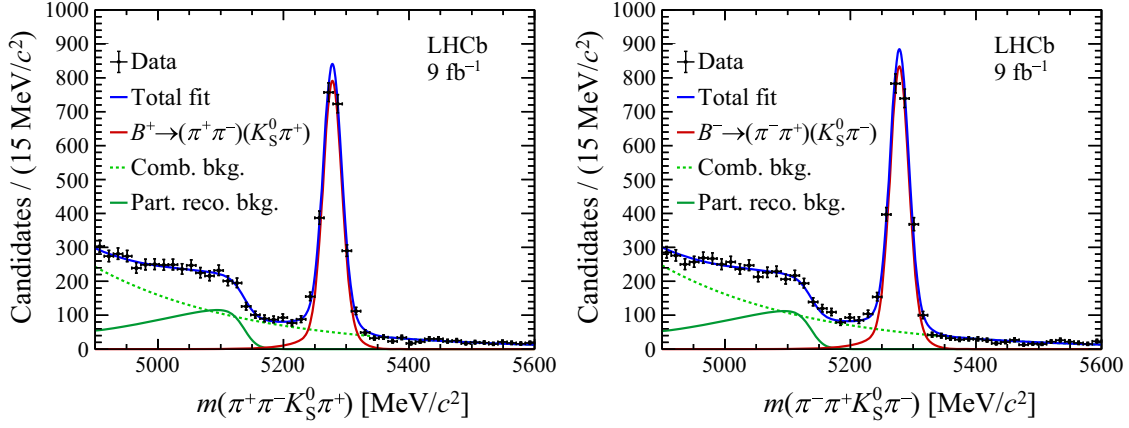


FIG. 1. Mass distributions of (left) $B^+ \rightarrow (\pi^+ \pi^-)(K_S^0 \pi^+)$ and (right) $B^- \rightarrow (\pi^- \pi^+)(K_S^0 \pi^-)$ candidates, with the fit results also shown.

defined as the angle between the momentum of the π^+ (K_S^0) in the $\pi^+ \pi^-$ ($K_S^0 \pi^+$) rest frame and the momentum of the ρ^0 (K^{*+}) meson in the B^+ rest frame. Following the isobar approach [66], the total amplitude of the

$B^+ \rightarrow (\pi^+ \pi^-)(K_S^0 \pi^+)$ consists of the coherent sum of quasi-two-body amplitudes. The differential decay rate for the B^+ decay is defined as the squared modulus of the total amplitude

$$\frac{d^5\Gamma}{d(m_{\pi^+\pi^-})d(m_{K_S^0\pi^+})d(\cos\theta_{\pi^+\pi^-})d(\cos\theta_{K_S^0\pi^+})d\phi} \propto \Phi \times \left| \sum_{i=1}^N A_i \times g_i(\cos\theta_{\pi^+\pi^-}, \cos\theta_{K_S^0\pi^+}, \phi) \times M_i(m_{\pi^+\pi^-}, m_{K_S^0\pi^+}) \right|^2, \quad (1)$$

where Φ is the four-body phase-space density and A_i is the complex coupling for each amplitude. By construction, the interference terms between components with different spin-parity quantum numbers cancel when integrating over the phase space. For the B^- decay, the sign of the ϕ angle is flipped and an independent set of complex couplings, \bar{A}_i , is measured. The g_i functions are characterized by spherical harmonics describing the angular distribution. The 22 amplitudes included in the baseline fit are detailed in Supplemental Material [67]. The M_i functions describe the mass distributions of the $\pi^+ \pi^-$ and $K_S^0 \pi^+$ systems. They are briefly described below and detailed in Supplemental Material [67].

In the $\pi^+ \pi^-$ mass spectrum, besides the $\rho(770)^0$ meson, a few other resonances are identified, including the $\omega(782)$, $f_0(500)$, $f_0(980)$, and $f_0(1370)$ mesons. The mass distributions of the vector resonances, $\rho(770)^0$ and $\omega(782)$, are modeled by a Gounaris-Sakurai parametrization [68] and a relativistic Breit-Wigner function, respectively. Those for the scalar resonances, $f_0(500)$ and $f_0(1370)$, are described by relativistic Breit-Wigner functions, while that for the $f_0(980)$ meson is modeled by a Flatté parametrization [69–71]. Several fits were performed with and without the scalar f_0 states; all states included in the baseline fit have an individual significance above 6 standard deviations. Alternative descriptions of the $\pi\pi$ S wave using the K -matrix formalism are considered as a source of systematic uncertainty, which is detailed below.

The $K_S^0 \pi^+$ mass distribution is dominated by the $K^*(892)^+$ resonance and a scalar contribution, referred to as the $(K_S^0 \pi^+)_S$ component. The $K^*(892)^+$ resonance is described by a relativistic Breit-Wigner. The $(K_S^0 \pi^+)_S$ distribution is parametrized by the LASS [72] model, which includes the contributions of the $K_0^*(1430)^+$ resonance and a broad low-mass component. Possible $(K_S^0 \pi^+)_P$ contributions from the $K_1(1270)$, $K_1(1400)$, and $K_1^*(1410)$ states were considered, but no significant effects are expected in the studied mass range. A small fraction of $B^+ \rightarrow a_1(1260)^+ K_S^0$ and $B^+ \rightarrow a_1(1640)^+ K_S^0$ decays is observed in the sample, with $a_1^+ \rightarrow \rho^0(\rightarrow \pi^+ \pi^-) \pi^+$, $a_1^+ \rightarrow f_0(500)(\rightarrow \pi^+ \pi^-) \pi^+$, and $a_1^+ \rightarrow f_0(980)(\rightarrow \pi^+ \pi^-) \pi^+$. The a_1 mass distributions are described by relativistic Breit-Wigner functions, with the angular variables redefined accordingly. Parameters describing the mass distributions are fixed in the baseline fit according to the results of previous measurements [15,38].

The combined probability-density function (PDF) for B^+ and B^- decays, composed of signal and background components, is given by

$$\mathcal{P}_{\text{tot}}(\vec{\mathcal{O}}, q; \{A_i, \bar{A}_i\}) = \frac{(1+q)\mathcal{P}_s + (1-q)\bar{\mathcal{P}}_s}{2 \int (\mathcal{P}_s + \bar{\mathcal{P}}_s) d\vec{\mathcal{O}}} (1 - r_b^+ - r_b^-) + \frac{(1+q)\mathcal{P}_b}{2 \int \mathcal{P}_b d\vec{\mathcal{O}}} r_b^+ + \frac{(1-q)\bar{\mathcal{P}}_b}{2 \int \bar{\mathcal{P}}_b d\vec{\mathcal{O}}} r_b^-, \quad (2)$$

where $q = \pm 1$ indicates the charge of the B^\pm meson, and r_b^\pm are background fractions fixed to the values obtained from the mass fit. The component $\mathcal{P}_s(\bar{\mathcal{P}}_s)$ is the differential decay rate described in Eq. (1) multiplied by the experimental efficiency for the B^+ (B^-) decay. The efficiency map as a function of the five kinematic variables is obtained by parametrizing the simulation sample using five-dimensional Legendre polynomials. Data-driven corrections are applied to the simulation to account for imperfections in the detector response and asymmetries in the detection efficiency of π^+ and π^- tracks. The background distributions, \mathcal{P}_b and $\bar{\mathcal{P}}_b$, for B^+ and B^- candidates, respectively, are

parametrized by five-dimensional Legendre polynomials using candidates in the high-mass region of the B^\pm spectra. The amplitude fit is performed simultaneously to the Run 1 and Run 2 samples. In the fit, the phase of each amplitude is measured relative to that of the $B^+ \rightarrow \rho^0(K_S^0\pi^+)_S$ component, which has a relatively large contribution. As the phase difference between B^+ and B^- is not observable, the phase of the $B^- \rightarrow \rho^0(K_S^0\pi^-)_S$ component is set to zero. The one-dimensional projections of the amplitude fit in the five kinematic variables are shown in Fig. 2. The CP asymmetry between the couplings of the $B^+ \rightarrow \rho^0(K_S^0\pi^+)_S$

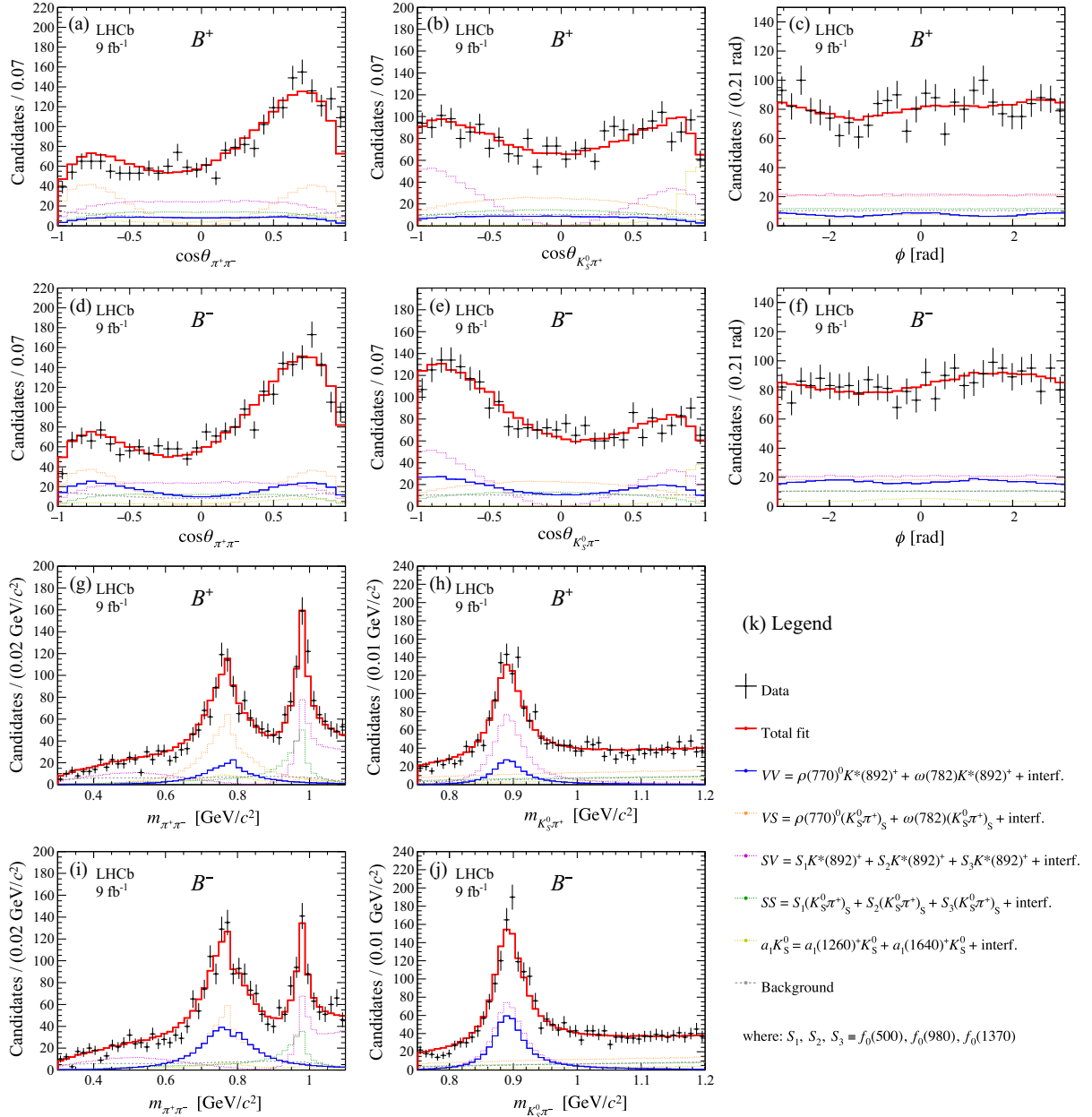


FIG. 2. Projections of the multidimensional amplitude fit onto (a) $\cos\theta_{\pi^+\pi^-}$, (b) $\cos\theta_{K_S^0\pi^+}$, (c) ϕ , (g) $m_{\pi^+\pi^-}$, and (h) $m_{K_S^0\pi^+}$ for the $B^+ \rightarrow (\pi^+\pi^-)(K_S^0\pi^+)$ decay. Plots (d)–(f), (i), (j) show the corresponding variables for the $B^- \rightarrow (\pi^+\pi^-)(K_S^0\pi^-)$ decay.

amplitude and its charge conjugate is found to be consistent with zero.

Two main categories of systematic uncertainty contribute to the result: those originating from experimental assumptions and those related to the amplitude model. The experimental category includes effects due to the limited precision of the background fractions, the efficiency map, and background modeling. The amplitude model uncertainties arise from limited knowledge of the fixed parameters of the resonance mass models, and possible spin-2 components neglected in the baseline fit. Systematic uncertainties due to experimental effects are found to be subdominant. The breakdown of the systematic uncertainties of observables is detailed in Table I of the End Matter. Results of the fitted parameters with their uncertainties are also summarized in Table II of the End Matter.

The experimental systematic uncertainty from the background fractions is evaluated by varying the r_b^\pm parameters within their uncertainties and repeating the amplitude fit. Systematic uncertainties due to the efficiency parametrization arise from imperfections of the five-dimensional efficiency map and from any residual charge-asymmetry effect. Imperfections are corrected by a weighting procedure to improve agreement with simulation across the five-dimensional space. The charge-asymmetry effects are assessed by deriving separate efficiency models for B^+ and B^- decays. To evaluate the uncertainty due to the background PDF, an alternative parametrization is obtained by combining B^+ and B^- samples or using samples with more relaxed selection criteria. Also, pseudoexperiments by bootstrapping the background sample [73] are used to extract the background PDF, where for each pseudoexperiment the amplitude fit is performed again. In each case, the deviation from the baseline result or the standard deviation of the results among the pseudoexperiments is taken as the corresponding systematic uncertainty.

The systematic uncertainty due to fixed parameters in the amplitude model is estimated using repeated fits to the data. Each time, the masses, widths, and hadron radii of intermediate resonances are varied within their uncertainties and an amplitude fit is performed under this model. The standard deviation of the distribution of the fit results among the repeated fits is taken as the corresponding systematic uncertainty. For the $B \rightarrow VV$ decay, the relative orbital angular momentum of the two vector mesons, L , could take the values $L = 0$ or $L = 2$ for the A_0 and A_{\parallel} amplitudes, and $L = 1$ for the A_{\perp} amplitude. Various L configurations are studied and the results are compared with that of the baseline fit with $L = 0$, and the largest difference is taken as the systematic uncertainty. The scalar component of the $\pi^+\pi^-$ mass spectrum can also be modeled using the K -matrix approach [74], as detailed in [75]. The difference between the results obtained with this alternative model and those from the baseline fit using explicit f_0 resonances is taken as a systematic uncertainty.

Furthermore, possible contributions of spin-2 resonances to the decay are assessed by including the $f_2(1270) \rightarrow \pi^+\pi^-$ or $K_2^*(1430)^+ \rightarrow K_S^0\pi^+$ components in the fit. The systematic uncertainties are estimated using the mean value of deviations, between the fits using extended model and baseline model, over an ensemble of pseudoexperiments.

The longitudinal polarization fraction averaged over the $B^+ \rightarrow \rho^0 K^{*+}$ and $B^- \rightarrow \rho^0 K^{*-}$ final states is determined in terms of the A_{λ} and \bar{A}_{λ} amplitudes, with $\lambda \in \{0, \parallel, \perp\}$, to be

$$f_L \equiv \frac{|A_0|^2 + |\bar{A}_0|^2}{\sum_{\lambda} (|A_{\lambda}|^2 + |\bar{A}_{\lambda}|^2)} = 0.720 \pm 0.028 \pm 0.009,$$

where, throughout this Letter, the first uncertainty is statistical and the second is systematic. The result is consistent with and more precise than the previous measurement [37]. The charge-specific quantities are determined to be

$$f_L^+ \equiv \frac{|A_0|^2}{\sum_{\lambda} |A_{\lambda}|^2} = 0.491 \pm 0.083 \pm 0.025,$$

$$f_L^- \equiv \frac{|\bar{A}_0|^2}{\sum_{\lambda} |\bar{A}_{\lambda}|^2} = 0.794 \pm 0.025 \pm 0.006.$$

The direct CP asymmetry for the total $B^+ \rightarrow \rho^0 K^{*+}$ decay rates [24,46] is measured to be

$$\mathcal{A}_{CP} \equiv \frac{\sum_{\lambda} (|\bar{A}_{\lambda}|^2 - |A_{\lambda}|^2)}{\sum_{\lambda} (|\bar{A}_{\lambda}|^2 + |A_{\lambda}|^2)} = 0.507 \pm 0.062 \pm 0.024.$$

The CP asymmetries are also determined for the magnitude and phase of each $B^+ \rightarrow \rho^0 K^{*+}$ amplitude. The results for the longitudinal component are

$$\mathcal{A}_{CP}(A_0) \equiv \frac{|\bar{A}_0|^2 - |A_0|^2}{|\bar{A}_0|^2 + |A_0|^2} = 0.664 \pm 0.083 \pm 0.029,$$

$$\Delta_{CP}(A_0) \equiv \arg(\bar{A}_0) - \arg(A_0) = 0.720 \pm 0.177 \pm 0.048 \text{ rad},$$

while the CP asymmetries of squared magnitudes and phases of A_{\parallel} and A_{\perp} components are measured to be

$$\mathcal{A}_{CP}(A_{\parallel}) = -0.063 \pm 0.137 \pm 0.027,$$

$$\Delta_{CP}(A_{\parallel}) = 0.477 \pm 0.187 \pm 0.114 \text{ rad},$$

$$\mathcal{A}_{CP}(A_{\perp}) = 0.284 \pm 0.140 \pm 0.051,$$

$$\Delta_{CP}(A_{\perp}) = 0.412 \pm 0.180 \pm 0.122 \text{ rad}.$$

Specifically, sizeable CP violation is observed for the magnitude of the longitudinal component, which drives the CP violation of the overall $B^+ \rightarrow \rho^0 K^{*+}$ decay rate. The phase difference between the longitudinal component of the $B^+ \rightarrow \rho^0 K^{*+}$ decay and its charge conjugate is 3.9 standard deviations away from zero, which suggests that

long-distance final-state interactions with other contributions in the phase space are playing a role in CP violation. The significance of CP violation for the $B^+ \rightarrow \rho^0 K^{*+}$ decay is quantified using a likelihood-ratio test [76] between the baseline fit, which allows for CP violation, and a CP -conserving model where the couplings of the $B^+ \rightarrow \rho^0 K^{*+}$ decay and its charge conjugate are constrained to be identical. The significance of a nonvanishing CP asymmetry is found to be above 9 standard deviations with systematic uncertainties taken into account. It marks the first observation of CP violation in this decay.

Triple product asymmetries (TPAs), which exploit the interference between two amplitudes, have been widely used to study CP violation for multibody decays. They are defined to be odd under both the time reversal and parity transformations. A nonzero TPA can either be due to a CP -violating phase or a CP -conserving phase induced by final-state interactions, referred to as the “true” and “fake” TPA, respectively. The true and fake TPAs are related to the couplings of the amplitudes [44,77] as

$$\begin{aligned} \mathcal{A}_{\text{true}}^{(1)} &\equiv -\frac{2\sqrt{2}}{\pi} \frac{\text{Im}(A_{\perp} A_0^* \mp \bar{A}_{\perp} \bar{A}_0^*)}{\sum_{\lambda \in \{0, \parallel, \perp\}} (|A_{\lambda}|^2 + |\bar{A}_{\lambda}|^2)}, \\ \mathcal{A}_{\text{true}}^{(2)} &\equiv -\frac{4}{\pi} \frac{\text{Im}(A_{\perp} A_{\parallel}^* \mp \bar{A}_{\perp} \bar{A}_{\parallel}^*)}{\sum_{\lambda \in \{0, \parallel, \perp\}} (|A_{\lambda}|^2 + |\bar{A}_{\lambda}|^2)}, \end{aligned} \quad (3)$$

where A_{λ}^* (\bar{A}_{λ}^*) denotes the complex conjugate of A_{λ} (\bar{A}_{λ}). Using the amplitude fit results, the TPAs are computed to be

$$\begin{aligned} \mathcal{A}_{\text{true}}^{(1)} &= -0.105 \pm 0.024 \pm 0.013, \\ \mathcal{A}_{\text{true}}^{(2)} &= 0.007 \pm 0.019 \pm 0.003, \\ \mathcal{A}_{\text{fake}}^{(1)} &= -0.157 \pm 0.024 \pm 0.011, \\ \mathcal{A}_{\text{fake}}^{(2)} &= 0.008 \pm 0.018 \pm 0.004. \end{aligned}$$

The true TPA $\mathcal{A}_{\text{true}}^{(1)}$ deviates from zero with a significance of approximately 4 standard deviations, indicating evidence of CP violation in interference. The fake TPA $\mathcal{A}_{\text{fake}}^{(1)}$ is nonzero with a significance of about 6 standard deviations, marking parity violation in interference [78].

In summary, an amplitude analysis of the decay $B^+ \rightarrow (\pi^+ \pi^-)(K_S^0 \pi^+)$ is performed within the mass ranges $0.30 < m_{\pi^+ \pi^-} < 1.10$ GeV/ c^2 and $0.75 < m_{K_S^0 \pi^+} < 1.20$ GeV/ c^2 . The longitudinal polarization and CP asymmetries are studied for the $B^+ \rightarrow \rho(770)^0 K^*(892)^+$ decay. The CP -averaged longitudinal fraction is measured to be $f_L = 0.720 \pm 0.028(\text{stat}) \pm 0.009(\text{syst})$. The direct CP asymmetry is determined to be $\mathcal{A}_{CP} = 0.507 \pm 0.062(\text{stat}) \pm 0.024(\text{syst})$, and the significance of CP violation is measured to exceed 9 standard deviations using a likelihood-ratio test. This is the first

observation of CP violation in the $B^+ \rightarrow \rho(770)^0 K^*(892)^+$ decay. These measurements are consistent with those previously reported by the BABAR Collaboration [37], with much better precision. The CP asymmetries are also derived for the magnitudes and phases of the three sub-amplitudes, suggesting that the longitudinal component drives the total CP violation. These results help to constrain theoretical models used to calculate B -hadron decays, shed light on the dynamics of heavy-flavor decays and contribute to the understanding of the polarization puzzle of B -meson decays.

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Data availability—The data that support the findings of this article are openly available [79].

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End Matter

The breakdown of systematic uncertainty contributions for the reported observables is shown in Table I.

Results of the fitted amplitude parameters, i.e., the real and imaginary parts of amplitude couplings, are summarized in Table II. Asymmetric uncertainties are evaluated

following the procedure described in Ref. [80]. Parameters marked with “...” are constrained in the fit, as explained below.

The reference amplitude is taken to be $A_{\rho(K_S^0\pi)_S}$, with couplings fixed to

TABLE I. Summary of the systematic uncertainty contributions for the reported observables, with statistical and total systematic uncertainties shown as reference. These uncertainties are given as absolute values.

	Statistical	Systematic (total)	Background fractions	Efficiency map	Background modeling	Mass models	Spin-2 components
\mathcal{A}_{CP}	0.062	0.024	0.0001	0.0049	0.0066	0.0216	0.0067
$\mathcal{A}_{CP}(A_0)$	0.083	0.029	0.0003	0.0061	0.0114	0.0206	0.0151
$\mathcal{A}_{CP}(A_{\parallel})$	0.137	0.027	0.0015	0.0040	0.0175	0.0166	0.0116
$\mathcal{A}_{CP}(A_{\perp})$	0.140	0.051	0.0005	0.0035	0.0158	0.0467	0.0116
$\Delta_{CP}(A_0)$	0.177	0.048	0.0031	0.0129	0.0304	0.0314	0.0141
$\Delta_{CP}(A_{\parallel})$	0.187	0.114	0.0040	0.0021	0.0138	0.1092	0.0282
$\Delta_{CP}(A_{\perp})$	0.180	0.122	0.0013	0.0053	0.0175	0.1145	0.0365

 TABLE II. Summary of the fitted real and imaginary parts of the amplitude couplings for the B^+ and B^- samples, respectively. The first uncertainties are statistical and the second ones are systematic. The reference amplitude is taken to be $A_{\rho(K_S^0\pi)_S}$. Parameters for the $a_1^+K_S^0$ components are reduced by constraining the CP -violating contributions to be the same among decay channels for each a_1 resonance, since its subdecays are CP -conserving strong interactions. These are signified with a “...” in the table.

Parameter	B^+		B^-			
$Re(A_{\rho(K_S^0\pi)_S})$...		0.9735	± 0.0314	± 0.0142	
$Im(A_{\rho(K_S^0\pi)_S})$	0 (Fixed)		0 (Fixed)			
$Re(A_{\rho K^*}^0)$	0.1641	± 0.0254	± 0.0415	0.2392	± 0.0332	± 0.0750
$Im(A_{\rho K^*}^0)$	0.0242	± 0.0266	± 0.0316	0.2811	± 0.0326	± 0.0779
$Re(A_{\rho K^*}^{\parallel})$	-0.1289	± 0.0141	± 0.0332	-0.1203	± 0.0143	± 0.0293
$Im(A_{\rho K^*}^{\parallel})$	0.0297	± 0.0184	± 0.0307	-0.0308	± 0.0180	± 0.0209
$Re(A_{\rho K^*}^{\perp})$	-0.1021	± 0.0142	± 0.0261	-0.1385	± 0.0133	± 0.0325
$Im(A_{\rho K^*}^{\perp})$	0.0246	± 0.0160	± 0.0249	-0.0246	± 0.0174	± 0.0248
$Re(A_{\omega K^*}^0)$	0.0005	± 0.0067	± 0.0059	-0.0087	± 0.0056	± 0.0034
$Im(A_{\omega K^*}^0)$	-0.0114	± 0.0058	± 0.0126	-0.0119	± 0.0074	± 0.0029
$Re(A_{\omega K^*}^{\parallel})$	-0.0023	± 0.0030	± 0.0009	-0.0006	± 0.0023	± 0.0005
$Im(A_{\omega K^*}^{\parallel})$	-0.0025	± 0.0028	± 0.0013	0.0020	± 0.0022	± 0.0007
$Re(A_{\omega K^*}^{\perp})$	-0.0001	± 0.0044	± 0.0014	-0.0027	± 0.0033	± 0.0008
$Im(A_{\omega K^*}^{\perp})$	-0.0042	± 0.0030	± 0.0013	0.0015	± 0.0034	± 0.0007
$Re(A_{\omega(K_S^0\pi)_S})$	0.0052	± 0.0112	± 0.0041	-0.0001	± 0.0119	± 0.0019
$Im(A_{\omega(K_S^0\pi)_S})$	0.0254	± 0.0096	± 0.0048	0.0276	± 0.0087	± 0.0026
$Re(A_{f_0(500)K^*})$	1.5539	± 0.1852	± 0.3636	1.0127	± 0.2455	± 0.2885
$Im(A_{f_0(500)K^*})$	0.3152	± 0.3778	± 0.2541	1.1808	± 0.2386	± 0.3634
$Re(A_{f_0(980)K^*})$	-0.1784	+0.0909 -0.1102	+0.1183 -0.1341	-0.4046	+0.0667 -0.1624	+0.0913 -0.1537
$Im(A_{f_0(980)K^*})$	-0.6713	+0.0811 -0.3013	+0.1309 -0.1595	-0.6048	+0.0824 -0.2850	+0.1284 -0.1519
$Re(A_{f_0(1370)K^*})$	0.5053	+0.3206 -0.3195	+0.2821 -0.2658	1.0462	+0.1879 -0.2688	+0.3300 -0.2286
$Im(A_{f_0(1370)K^*})$	0.1557	+0.2860 -0.2424	+0.1668 -0.1855	0.4208	+0.2378 -0.2555	+0.2246 -0.2077
$Re(A_{f_0(500)(K_S^0\pi)_S})$	0.6749	± 0.4192	± 0.2929	1.3057	± 0.3611	± 0.2671
$Im(A_{f_0(500)(K_S^0\pi)_S})$	-0.3747	± 0.4989	± 0.2675	-0.1689	± 0.5528	± 0.2425
$Re(A_{f_0(980)(K_S^0\pi)_S})$	-0.2698	+0.0870 -0.2642	+0.1513 -0.1596	-0.3532	+0.0924 -0.2573	+0.0725 -0.0790
$Im(A_{f_0(980)(K_S^0\pi)_S})$	1.3567	+0.6411 -0.2222	+0.3352 -0.3304	0.9319	+0.4909 -0.1349	+0.3050 -0.3044
$Re(A_{f_0(1370)(K_S^0\pi)_S})$	1.3511	+0.5718 -0.5138	+0.5271 -0.5279	0.2864	+0.5436 -0.5300	+0.4094 -0.4008
$Im(A_{f_0(1370)(K_S^0\pi)_S})$	0.1008	+1.0180 -0.4300	+0.6857 -0.6563	0.5882	+0.4970 -0.4542	+0.3376 -0.3491
$Re(A_{(a_1(1260)\rightarrow\rho\pi)K_S^0}^0)$	-2.5802	± 1.3487	± 2.2671	-2.0785	± 0.6787	± 0.9635

(Table continued)

TABLE II. (Continued)

Parameter	B^+			B^-		
$\mathcal{I}m(A_{(a_1(1260)\rightarrow\rho\pi)K_S^0}^0)$	-0.5676	± 0.9027	± 1.1999	-0.8797	± 0.6419	± 0.8860
$\mathcal{R}e(A_{(a_1(1260)\rightarrow\rho\pi)K_S^0}^{\parallel})$...			-0.1507	± 1.5943	± 0.8448
$\mathcal{I}m(A_{(a_1(1260)\rightarrow\rho\pi)K_S^0}^{\parallel})$...			3.0275	± 1.3924	± 1.4278
$\mathcal{R}e(A_{(a_1(1260)\rightarrow f_0(500)\pi)K_S^0})$...			-8.5584	+1.8330 -1.8408	+4.2256 -3.9197
$\mathcal{I}m(A_{(a_1(1260)\rightarrow f_0(500)\pi)K_S^0})$...			3.5230	+1.2376 -0.7814	+2.0371 -2.0247
$\mathcal{R}e(A_{(a_1(1260)\rightarrow f_0(980)\pi)K_S^0})$...			1.2407	+0.8240 -1.2627	+1.3965 -1.3885
$\mathcal{I}m(A_{(a_1(1260)\rightarrow f_0(980)\pi)K_S^0})$...			0.7200	+0.8666 -1.0314	+0.4065 -0.4259
$\mathcal{R}e(A_{(a_1(1640)\rightarrow\rho\pi)K_S^0}^0)$	-0.3555	± 0.4472	± 0.3954	-0.2564	± 0.4432	± 0.3951
$\mathcal{I}m(A_{(a_1(1640)\rightarrow\rho\pi)K_S^0}^0)$	-0.0363	± 0.5007	± 0.3456	-0.0859	± 0.3758	± 0.2064
$\mathcal{R}e(A_{(a_1(1640)\rightarrow\rho\pi)K_S^0}^{\parallel})$...			-0.3892	± 0.8504	± 0.5404
$\mathcal{I}m(A_{(a_1(1640)\rightarrow\rho\pi)K_S^0}^{\parallel})$...			-0.2174	± 0.9290	± 0.9068
$\mathcal{R}e(A_{(a_1(1640)\rightarrow f_0(500)\pi)K_S^0})$...			3.8584	± 1.3145	± 1.4161
$\mathcal{I}m(A_{(a_1(1640)\rightarrow f_0(500)\pi)K_S^0})$...			0.5558	± 1.1537	± 1.6115
$\mathcal{R}e(A_{(a_1(1640)\rightarrow f_0(980)\pi)K_S^0})$...			-0.3569	+0.6560 -0.7193	+1.1383 -1.1493
$\mathcal{I}m(A_{(a_1(1640)\rightarrow f_0(980)\pi)K_S^0})$...			-1.7988	+0.6287 -0.6458	+1.1608 -1.1620

$$\begin{aligned}
 B^+ : \mathcal{R}e(A_{\rho(K_S^0\pi)_S}^+) &= 1 - \Delta, & \mathcal{I}m(A_{\rho(K_S^0\pi)_S}^+) &= 0, \\
 B^- : \mathcal{R}e(A_{\rho(K_S^0\pi)_S}^-) &= 1 + \Delta, & \mathcal{I}m(A_{\rho(K_S^0\pi)_S}^-) &= 0, \quad (A1)
 \end{aligned}$$

$$\frac{A_0^+}{A_0^-} = \frac{A_1^+}{A_1^-} = \frac{A_2^+}{A_2^-} = \frac{A_3^+}{A_3^-}, \quad (A2)$$

where Δ describes the CP asymmetry of the reference amplitude. In the fit, $\mathcal{R}e(A_{\rho(K_S^0\pi)_S}^+)$ is thus constrained to be $2 - \mathcal{R}e(A_{\rho(K_S^0\pi)_S}^-)$.

For each a_1 resonance, the decays $a_1 \rightarrow X\pi$ [$X = \rho, f_0(500), f_0(980)$] proceed via CP -conserving strong interactions. The CP -violating contributions are therefore shared among all $B \rightarrow a_1 K_S^0$ channels, where a_1 denotes $a_1(1260)^+$ or $a_1(1640)^+$. The four amplitudes satisfy

with

$$\begin{aligned}
 A_0 &= A_{a_1(\rightarrow\rho\pi)K_S^0}^0, & A_1 &= A_{a_1(\rightarrow\rho\pi)K_S^0}^{\parallel}, \\
 A_2 &= A_{a_1(\rightarrow f_0(500)\pi)K_S^0}, & A_3 &= A_{a_1(\rightarrow f_0(980)\pi)K_S^0}. \quad (A3)
 \end{aligned}$$

In the fit, A_0^+ and all $A_{i=0,1,2,3}^-$ are free parameters, while the other $A_{i=1,2,3}^+$ are constrained through these relations.

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