

The formation and coalescence sites of the first gravitational wave events

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ABSTRACT

We present a novel theoretical model to characterize the formation and coalescence sites of compact binaries in a cosmological context. This is based on the coupling between the binary population synthesis code *SeBa* with a simulation following the formation of a Milky Way-like halo in a well-resolved cosmic volume of 4 cMpc, performed with the *GAMESH* pipeline. We have applied this technique to investigate when and where systems with properties similar to the recently observed LIGO/VIRGO events are more likely to form and where they are more likely to reside when they coalesce. We find that more than 70 per cent of GW151226 and LVT151012-like systems form in galaxies with stellar mass $M_* > 10^8 M_\odot$ in the redshift range [0.06–3] and [0.14–11.3], respectively. All GW150914-like systems form in low-metallicity dwarfs with $M_* < 5 \times 10^6 M_\odot$ at $2.4 \leq z \leq 4.2$. Despite these initial differences, by the time they reach coalescence the observed events are most likely hosted by star-forming galaxies with $M_* > 10^{10} M_\odot$. Due to tidal stripping and radiative feedback, a non-negligible fraction of GW150914-like candidates end-up in galaxies with properties similar to dwarf spheroidals and ultrafaint satellites.

Key words: black hole physics – gravitational waves – binaries: close – stars: black holes – galaxies: evolution – galaxies: high-redshift.

1 INTRODUCTION

The recent detection of gravitational waves from the LIGO/VIRGO collaboration has opened a new era of gravitational wave astronomy (Abbott et al. 2016a; Abbott et al. 2016b). During the first Advanced LIGO observing run (hereafter O1, from 2015 September 12 to 2016 January 19), two sources have been unambiguously detected (GW150914 and GW151226), while a third one (LVT151012) was below detection threshold, but with 87 per cent probability of being of astrophysical origin (Abbott et al. 2016c). At the time of submission of this Letter, the detection of a fourth event has been reported, GW170104¹ (Abbott et al. 2017).

All the four sources are powered by the inspiral and coalescence of two black holes (BHs) and the binary properties, estimated from the gravitational wave signals, have profound astrophysical implications (Abbott et al. 2016d). In particular, GW150914 originated from the merger of two $\sim 30 M_\odot$ BHs at $z \sim 0.09$, suggesting that stellar BHs with such large masses can form in nature, evolve in a binary system and coalesce within a Hubble time. Comparison with stellar and binary evolution models suggests progeni-

tor stars with low metallicity, $Z < 0.5 Z_\odot$ (Abbott et al. 2016a; Belczynski et al. 2016; Mapelli 2016). In fact, reduced mass loss at low metallicity favors the formation of more massive stellar remnants (Mapelli, Colpi & Zampieri 2009; Belczynski et al. 2010; Mapelli et al. 2010; Spera, Mapelli & Bressan 2015).

The limit on the metallicity potentially provides very interesting constraints on the birth environment of massive BH binaries. If the binary BH system has merged in a short time, it must have formed in a rare, low-metallicity dwarf galaxy. Alternatively, in the long merger time scenario (> 9 Gyr), it could have formed at high redshift ($z > 2$), where low-metallicity star formation is expected to be more common (Abbott et al. 2016d).

The main goal of this paper is to investigate when and where massive BH binary systems with properties similar to GW150914, GW151226 and LVT151012 are more likely to form, and where they are more likely to reside at the time of their coalescence.

Following its discovery, several attempts have been made to determine the environment in which GW150914 formed. Belczynski et al. (2016) and Dvorkin et al. (2016) use different massive BH formation scenarios and the observationally inferred cosmic star formation rate density evolution with a metallicity-dependent correction to estimate the redshift evolution of birth and merger rate of massive BH binaries. Although these studies

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¹ The analysis presented is limited to the first three events.

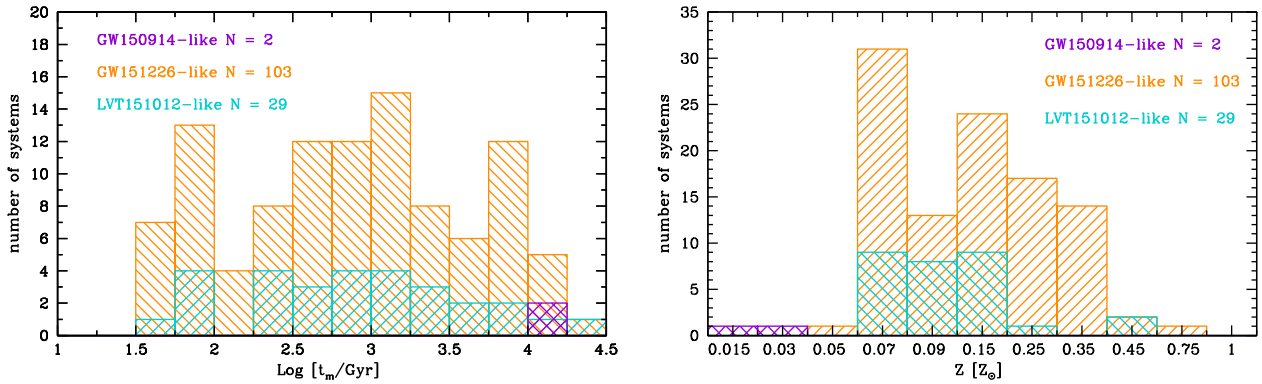


Figure 1. The number of events like GW150914, GW151226 and LVT151012 (see the legend) predicted by `SeBa` as a function of metallicity (left-hand panel) and merger time (right-hand panel).

may provide useful constraints on the redshift dependent birth and merger histories of compact binary systems, (Schneider et al. 2001; Marassi et al. 2011; Regimbau 2011; Dominik et al. 2013), they are not capable of discriminating individual formation or coalescence sites. Using observationally inferred galaxy scaling relations Lamberts et al. (2016) and Elbert, Bullock & Kaplinghat (2017) predict the low redshift BH binary merger rate as a function of the present-day host galaxy mass. They find that GW150914-like events with short merger time-scales would be primarily localized in dwarf galaxies, and in massive galaxies otherwise. Conversely, using cosmological simulations of galaxies with different masses at $z = 0$, O’Shaughnessy et al. (2016) find that a present-day dwarf galaxy can host a considerably larger BH binary merger rate compared to a massive galaxy. However, some of the galaxy scaling relations adopted by Lamberts et al. (2016) are not directly observed for low-mass faint galaxies, and are therefore based on extrapolations. This may introduce considerable uncertainties in the estimated properties of the most likely sites of low-metallicity star formation, hence of binary BH formation. The analyses of O’Shaughnessy et al. (2016) and Elbert et al. (2017) adopt a delay time distribution function to characterize the merger time of binary BHs and do not determine the properties of individual binary systems formed in each galaxy.

In this work, we attempt to overcome the above limitations, and to use individual galaxy properties to predict the number and properties of binary systems that each galaxy hosts.

2 FORMING BH–BH SYSTEMS

2.1 The binary population synthesis model

We adopt the binary population synthesis code `SeBa`² originally developed by Portegies Zwart & Verbunt (1996) and Nelemans, Yungelson & Portegies Zwart (2001). `SeBa` follows the evolution of binary systems by taking into account the relevant physics involved in their evolution: stellar composition, stellar winds, mass transfer and accretion, magnetic braking, common envelope phase, supernova kicks and gravitational radiation. The original version has been recently modified by Mapelli et al. (2013) to include metallicity-dependent prescriptions for stellar evolution, stellar winds and remnant formation. In particular, metallicity-dependent stellar evolution is based on the polynomial fitting formulas described in Hurley,

Pols & Tout (2000). Stellar winds were substantially upgraded including Vink, de Koter & Lamers (2001) prescriptions for O-type massive stars, Vink & de Koter (2005) formalism for Wolf–Rayet stars, and Belczynski et al. (2010) recipes for luminous blue variable stars. The mass of the compact remnant was derived as described in Mapelli et al. (2009): stars with a pre-supernova mass $> 40 M_{\odot}$ are assumed to collapse to BH directly, retaining most of their final mass. Binary evolution was modelled as in the default `SeBa` code. For more details on single and binary evolution, see Mapelli et al. (2013) and fig. 1 of Mapelli et al. (2013) for the derived BH mass spectrum. We set the binary fraction $f_{\text{bin}} = 1$ so that all the stars are assumed to be in binary systems. Observations show that this assumption is approximately correct for stars with masses $> 10 M_{\odot}$ (Sana et al. 2012). For each simulation, we initialize $N = 2 \times 10^6$ binaries and follow their evolution with initial properties randomly selected from independent distribution functions. In particular, the primary stellar mass, m_p , is distributed according to a Kroupa Initial Mass Function (IMF; Kroupa 2001) between $[0.1–100] M_{\odot}$. The mass of the secondary star, m_s , is generated according to a flat distribution for the mass ratio $q = m_s/m_p$ with $0.1 < q \leq 1$. The initial semimajor axis (sma) distribution is flat in $\log(\text{sma})$ (see Portegies Zwart & Verbunt 1996) ranging from $0.1 R_{\odot}$ (Roche lobe contact) up to $10^6 R_{\odot}$. The eccentricity of the binary is selected from a thermal distribution $f(e) = 2e$ in the $[0–1]$ range (Heggie 1975). With this choice of initial conditions, we run simulations for 11 different values of the initial metallicity in the range $0.01 Z_{\odot} \leq Z \leq 1 Z_{\odot}$.

An extended statistical analysis of the simulations will be presented in a forthcoming paper. Here we illustrate the properties of simulated BH–BH systems with primary and secondary masses in the range estimated for GW150914 ($m_{\text{BH,p}} = 36.2^{+5.2}_{-3.8} M_{\odot}$ and $m_{\text{BH,s}} = 29.1^{+3.7}_{-4.4} M_{\odot}$), GW151226 ($m_{\text{BH,p}} = 14.2^{+8.3}_{-3.7} M_{\odot}$ and $m_{\text{BH,s}} = 7.5^{+2.3}_{-2.3} M_{\odot}$) and LVT151012 ($m_{\text{BH,p}} = 23^{+18}_{-6} M_{\odot}$ and $m_{\text{BH,s}} = 13^{+4}_{-5} M_{\odot}$). In the left-hand panel of Fig. 1, we show the number of candidate systems for the three events found in simulated samples with different metallicities. We find only two massive BH binaries with masses compatible with GW150914 and both require very low initial stellar metallicities, $Z < 0.05 Z_{\odot}$.³ GW151226-like systems are more common and their stellar progenitors have metallicities in the range $0.05 Z_{\odot} \leq Z \leq 0.75 Z_{\odot}$. Due to the higher mass of the primary BH, we find that LVT151012-like

³ A similar condition ($Z < 0.07 Z_{\odot}$) applies to GW170104-like systems, given the masses of the primary ($m_{\text{BH,p}} = 31.2^{+8.4}_{-6} M_{\odot}$) and secondary ($m_{\text{BH,s}} = 19.4^{+5.3}_{-5.9} M_{\odot}$) black holes.

² <http://www.sns.ias.edu/starlab/seba/>

systems are less frequent and that most of their stellar progenitors have metallicities $0.07 Z_{\odot} \leq Z \leq 0.25 Z_{\odot}$. In the right-hand panel of Fig. 1, we show the corresponding distribution of merger times. The two GW150914-like systems are both characterized by long coalescence times $3.87 < \lg(t_m/\text{Gyr}) < 4.12$. This is expected as massive BH binaries originate from massive stellar binaries that, given their larger radii, must have large semimajor axis at birth to avoid merging before the compact binary system forms (Linden et al. 2010; Mapelli & Zampieri 2014; Ziosi et al. 2014). Instead, GW151226 and LVT151012-like systems follow a relatively flat distribution in merger times in the range $1.37 < \lg(t_m/\text{Gyr}) \leq 4.25$. Due to the initial mass ratio in the zero age main sequence ($0.4 \leq q < 0.6$), all the GW151226 and LVT151012-like systems during their evolution go through a phase of common envelope, which drastically reduces the initial orbital separation. For these systems, the flat merger times distribution is a consequence of the flat initial distribution of orbital separations.

2.2 The cosmological simulation

We couple the binary information provided by *SeBa* with the star formation and chemical enrichment histories of all the galaxies contained in a comoving volume $(4 \text{ cMpc})^3$, experiencing a forming Milky Way (MW)-like galaxy at its centre. These are obtained processing an *N*-Body cosmological simulation with the *GAMESH* pipeline (Graziani et al. 2015). The simulation has been presented in Graziani et al. (2017) and here we briefly summarize the properties relevant to the present analysis.

The *N*-Body simulation is performed by the code *GCD+* (Kawata et al. 2013) and adopts a Planck 2013 cosmology (Planck Collaboration XVI 2014, $\Omega_m = 0.32$, $\Omega_{\Lambda} = 0.68$, $\Omega_b = 0.049$ and $h = 0.67$) and initial conditions (ICs) suitable to reproduce an MW-like halo in the present Universe, starting from a cosmological volume of about $(83.53 \text{ cMpc})^3$. Once an MW-sized halo is identified at the largest scale, we re-create ICs for a multiresolution, zoom-in simulation resolving the same halo with mass $M_{\text{MW}} = 1.7 \times 10^{12} M_{\odot}$ at the centre of a volume of $(4 \text{ cMpc})^3$ with a dark matter particle resolution mass of $3.4 \times 10^5 M_{\odot}$. Hereafter we will refer to this volume as the Local Group (LG) of the MW-like halo. The simulation runs from $z = 20$ to $z = 0$ and we store the outputs with a time resolution of 15 Myr at $z > 10$, and of 100 Myr at $z \leq 10$. In each snapshot, haloes are identified by a standard Friend-of-Friend algorithm adopting linking parameter of $b = 0.2$ and a minimum number of particles of 100. A particle-based merger tree (MT) has been computed to exactly establish each halo ancestor/descendant relationships, also accounting for all the dynamical processes regulating halo assembly: accretion, mergers, tidal stripping and halo disruption. The simulation is in good agreement with observations and with independent theoretical studies (Graziani et al. 2017). At all redshifts, the resulting halo mass function in the LG matches the prediction of the analytic Press–Schechter distribution for all haloes with $M \leq 10^{10} M_{\odot}$. Below $z \sim 3$, the central halo dynamically dominates the LG region (half of the MW halo mass is already assembled by $z \sim 1.5$) and haloes with mass $M > [10^{10} - 10^{11}] M_{\odot}$ are found to evolve faster than expected for an average cosmic epoch.

The baryonic evolution of galaxies is performed by *GAMESH* accounting for star formation, metal enrichment, Pop III/Pop II transition and supernova (SN)-driven feedback. Radiative feedback is modelled by adopting an instant reionization prescription which suppresses star formation in all galaxies hosted by mini-haloes (with virial temperatures $T_{\text{vir}} < 10^4 \text{ K}$) found at $z \leq 6$. By calibrating the model free parameters to reproduce the stellar, gas and metal mass

observed in the MW, we find the simulated galaxies to be in good agreement with recent observations of candidate MW progenitors at $0 < z < 2.5$, with the galaxy main sequence, mass-metallicity relation and Fundamental Plane of metallicity relations in the redshift range $0 < z < 4$.

It is worth pointing out that although the simulated cosmic volume is very small compared to the current instrumental range of the advanced LIGO detector ($d \leq 1 \text{ Gpc}$), the adopted resolution allows us to simulate DM structures down to a minimum mass of $\sim 3.4 \times 10^7 M_{\odot}$, where star formation in low-metallicity environments (hence massive BH formation) is more likely to occur.

2.3 BH binary formation in the simulated galaxies

In order to determine the properties of compact binaries formed in each galaxy, we assume that the stellar progenitors have the metallicity of the gas in which they form and we randomly extract from the *SeBa* output with the closest metallicity a number of binary systems until we reach the total mass of newly formed stars predicted by the cosmological simulation. As a result of this procedure, we can predict the metallicity-dependent formation and merger rates of compact binaries and the properties of compact binary systems hosted in each galaxy of the LG at any given time from $0 \leq z \leq 20$.

3 RESULTS

We select, among all the simulated binaries, systems with properties consistent with GW150914, GW151226 and LVT151012. This is done by requiring that the system has primary and secondary BH masses in the observed range and that it coalesces at $z_m = 0.09^{+0.03}_{-0.04}$ for GW150914 and GW151226, and at $z_m = 0.20^{+0.09}_{-0.09}$ for LVT151012. We find $N = 11, 9382$ and 8958 for GW150914, GW151226 and LVT151012, corresponding to merger rates, in the LG, of $\sim 0.2, 162$ and $70 \text{ Gpc}^{-3} \text{ yr}^{-1}$, respectively. These differ from the rates obtained by Abbott et al. (2016c) based on populations with masses matching the observed events and assuming a uniform distribution in comoving volume.⁴ Indeed, for this comparison to be meaningful a larger simulation box probing a more representative cosmological volume should be considered (see Mapelli et al. 2017 for a similar approach using the *Illustris* simulation).

For each class of systems, we reconstruct from the simulation output the properties of their formation and coalescence sites. Fig. 2 shows the redshift distribution (left-hand panel) and the mass-metallicity relation (right-hand panel) of the host galaxies at BH binary formation. The redshift range over which the systems formed reflects the corresponding merger time distribution. GW150914-like systems are characterized by long merger times and form in the range $2.36 \leq z_f \leq 4.15$. GW151226 and LVT151012-like systems, which have a broad range of possible merger times, can form in relatively wide redshift intervals $0.06 \leq z_f \leq 2.97$ and $0.14 \leq z_f \leq 11.3$, respectively. However, we find that while only 6 per cent of GW151226-like systems have $z_f > 2$, among LVT151012 systems, 67 per cent have $z_f > 2$, 48 per cent have $z_f > 4$ and 6 per cent formed in the pre-reionization epoch, with $z_f > 6$. In addition, all the GW150914-like systems are born in low-metallicity dwarfs with stellar mass $M_* < 5 \times 10^6 M_{\odot}$, while 88 per cent (70 per cent)

⁴ Abbott et al. (2016c) find $3.4^{+8.8}_{-2.8}, 36^{+95}_{-30}$ and $9.1^{+31}_{-8.5} \text{ Gpc}^{-3} \text{ yr}^{-1}$ for GW150914, GW151226 and LVT151012, where we quote the median values with 90 per cent confidence from their Table II.

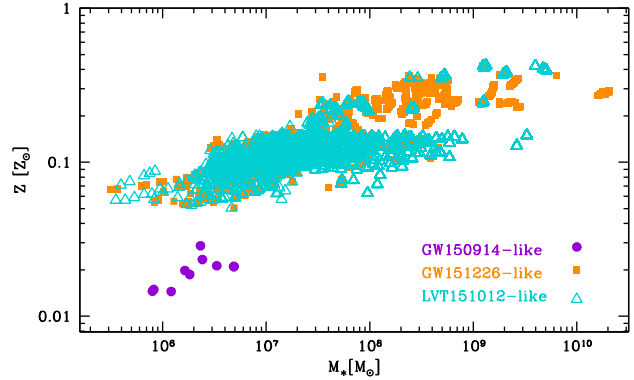
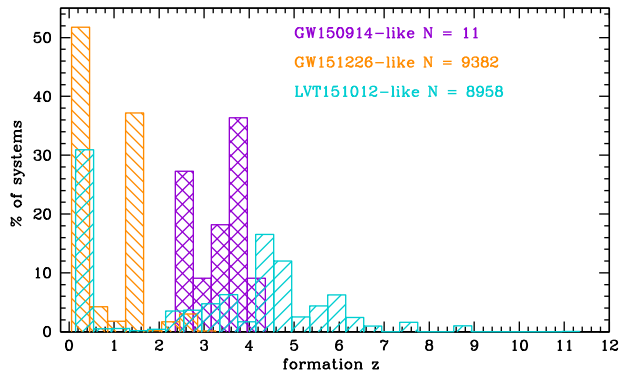


Figure 2. Properties of the formation sites of GW150914, GW151226 and LVT151012-like systems in the simulation. Left-hand panel: percentage of systems as a function of formation redshift. Right-hand panel: gas metallicity as a function of the stellar mass of the galaxies where the simulated LIGO-like events are formed.

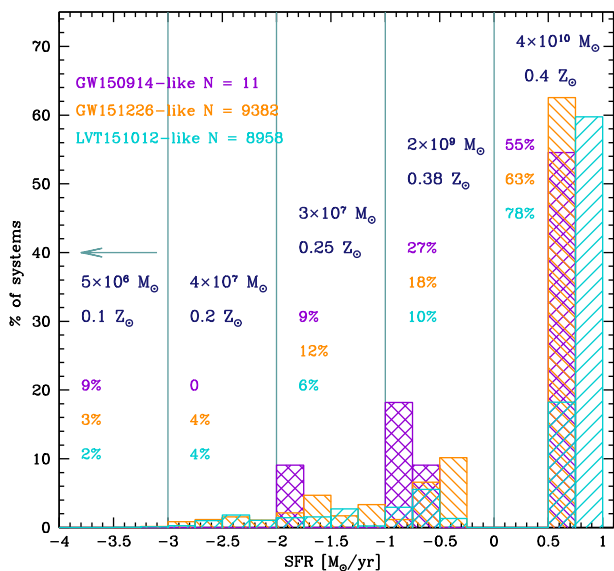


Figure 3. Properties of the coalescence sites of GW150914, GW151226 and LVT151012-like systems in the simulation. Histograms show the percentage of systems hosted in galaxies binned by their star formation rate at the time of coalescence. The percentage of BH binaries hosted in galaxies with SFRs within the broader bins identified by the vertical lines are also shown, together with the average host stellar mass and metallicity. The numbers in the leftmost bin refer to BH binaries hosted in galaxies with negligible or null star formation activity, as indicated by the arrow (see the text).

of GW151226 (LVT151012)-like systems form in galaxies with $M_* > 10^8 M_\odot$.

We track each GW150914, GW151226 and LVT151012-like BH system from formation to coalescence using the particle-based MT and we identify the galaxy where it resides when the merger event occurs. The results of this procedure are illustrated in Fig. 3. The histograms represent the percentage of systems hosted in galaxies characterized by their star formation rate (SFR) at the time of coalescence. The numbers shown in the plot refer to the percentage of systems in larger SFR intervals as identified by the vertical lines. For each of these intervals, we also report the average stellar mass and metallicity of the hosts. The numbers in the leftmost bin refer to systems which are not forming stars at the time of coalescence. Our results suggest that GW150914, GW151226 and LVT151012-like systems have the largest probability to be hosted in galaxies with

masses $M_* \sim 4 \times 10^{10} M_\odot$, metallicities $Z \sim 0.4 Z_\odot$ and which form stars at moderate rates $\sim 5 M_\odot \text{ yr}^{-1}$. These are the progenitors of the MW-like galaxy at the redshift of coalescence (Graziani et al. 2017). Smaller galaxies, with stellar masses encompassing the range of LMC, SMC and dwarfs, have a smaller probability to have hosted the first three GW events.

Finally, we find a small but not negligible percentage of GW150914-like systems (~ 10 per cent) whose coalescence could be hosted in very small galaxies, with $M_* \sim 5 \times 10^6 M_\odot$, where star formation has been suppressed by radiative feedback. These BH binaries have formed in dwarf galaxies at $z \sim 4$ which, as a consequence of stripping events, lower their (dark and baryonic) mass below the limit that renders gas infall unfavorable (virial temperatures smaller than $\sim 2 \times 10^4 \text{ K}$) in the rising UV background accompanying reionization. Although these findings are based on a very small number statistic (1 out of 11 GW150914-like systems), they suggest that the hosts of massive BH binary mergers might be similar to the least massive among dwarf spheroidals or to the more massive among ultrafaint galaxies.

4 CONCLUSIONS

The work that we have presented is only the first step towards a more extended analysis of different classes of compact binary systems and their detectability as gravitational wave sources. Ultimately, our goal is to predict the most probable sites of formation and coalescence of different classes of compact binary systems. This information will help the search for the host galaxy properties and to identify the electromagnetic counterparts of some gravitational wave sources.

While we plan to present an extended analysis in future work, here we select, among all the simulated binaries, GW150914, GW151226 and LVT151012-like systems. We find that, despite the fact that these systems require different galaxy properties at the time of their formation, they all have a larger probability to be hosted in massive, star-forming galaxies at the time of their coalescence. This is in agreement with what was recently suggested by independent studies (Lamberts et al. 2016; Elbert et al. 2017). However, massive BH binaries which preferentially form in metal-poor dwarfs at $2.5 \leq z \leq 4.2$, can also fail to be incorporated in more massive galaxies during hierarchical evolution. As a result, they might have evolved within galaxies which are fragile to radiative feedback effects, reaching coalescence in small non-star-forming dwarf satellites.

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