

# Measurement of the $CP$ Violation Parameter $A_\Gamma$ in $D^0 \rightarrow K^+K^-$ and $D^0 \rightarrow \pi^+\pi^-$ Decays

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Asymmetries in the time-dependent rates of  $D^0 \rightarrow K^+K^-$  and  $D^0 \rightarrow \pi^+\pi^-$  decays are measured in a  $pp$  collision data sample collected with the LHCb detector during LHC Run 1, corresponding to an integrated luminosity of  $3 \text{ fb}^{-1}$ . The asymmetries in effective decay widths between  $D^0$  and  $\bar{D}^0$  decays, sensitive to indirect  $CP$  violation, are measured to be  $A_\Gamma(K^+K^-) = (-0.30 \pm 0.32 \pm 0.10) \times 10^{-3}$  and  $A_\Gamma(\pi^+\pi^-) = (0.46 \pm 0.58 \pm 0.12) \times 10^{-3}$ , where the first uncertainty is statistical and the second systematic. These measurements show no evidence for  $CP$  violation and improve on the precision of the previous best measurements by nearly a factor of two.

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Symmetry under the combined operations of charge conjugation and parity ( $CP$ ) was found to be violated in flavor-changing interactions of the  $s$  quark [1], and later in processes involving the  $b$  quark [2,3]. Within the standard model, violation of  $CP$  symmetry in the charm sector is predicted at a level below  $\mathcal{O}(10^{-3})$  [4,5]. Charm hadrons are the only particles where  $CP$  violation involving up-type quarks is expected to be observable, providing a unique opportunity to detect effects beyond the standard model that leave down-type quarks unaffected.

A sensitive probe of  $CP$  violation in the charm sector is given by decays of  $D^0$  mesons into  $CP$  eigenstates  $f$ , where  $f = \pi^+\pi^-$  or  $f = K^+K^-$ . The time-integrated  $CP$  asymmetries and the charm-mixing parameters  $x \equiv (m_2 - m_1)/\Gamma$  and  $y \equiv (\Gamma_2 - \Gamma_1)/(2\Gamma)$  [6], where  $m_{1,2}$  and  $\Gamma_{1,2}$  are the masses and widths of the mass eigenstates  $|D_{1,2}\rangle$ , are known to be small [7–9]. As a result, the time-dependent  $CP$  asymmetry of each decay mode can be approximated as [8]

$$A_{CP}(t) \equiv \frac{\Gamma(D^0(t) \rightarrow f) - \Gamma(\bar{D}^0(t) \rightarrow f)}{\Gamma(D^0(t) \rightarrow f) + \Gamma(\bar{D}^0(t) \rightarrow f)} \approx a_{\text{dir}}^f - A_\Gamma \frac{t}{\tau_D}, \quad (1)$$

where  $\Gamma(D^0(t) \rightarrow f)$  and  $\Gamma(\bar{D}^0(t) \rightarrow f)$  indicate the time-dependent decay rates of an initial  $D^0$  or  $\bar{D}^0$  decaying to a final state  $f$  at decay time  $t$ ,  $\tau_D = 1/\Gamma = 2/(\Gamma_1 + \Gamma_2)$  is the average lifetime of the  $D^0$  meson,  $a_{\text{dir}}^f$  is the asymmetry

related to direct  $CP$  violation, and  $A_\Gamma$  is the asymmetry between the  $D^0$  and  $\bar{D}^0$  effective decay widths

$$A_\Gamma \equiv \frac{\hat{\Gamma}_{D^0 \rightarrow f} - \hat{\Gamma}_{\bar{D}^0 \rightarrow f}}{\hat{\Gamma}_{D^0 \rightarrow f} + \hat{\Gamma}_{\bar{D}^0 \rightarrow f}}. \quad (2)$$

The effective decay width  $\hat{\Gamma}_{D^0 \rightarrow f}$  is defined as  $\int_0^\infty \Gamma(D^0(t) \rightarrow f) dt / \int_0^\infty t \Gamma(D^0(t) \rightarrow f) dt$ , i.e., the inverse of the effective lifetime.

Neglecting contributions from subleading amplitudes [5,10],  $a_{\text{dir}}^f$  vanishes and  $A_\Gamma$  is independent of the final state  $f$ . Furthermore, in the absence of  $CP$  violation in mixing, it can be found that  $A_\Gamma = -x \sin \phi$ , where  $\phi = \arg[(q\bar{A}_f)/(pA_f)]$ ,  $A_f(\bar{A}_f)$  is the amplitude of the  $D^0 \rightarrow f$  ( $\bar{D}^0 \rightarrow f$ ) decay, and  $p$  and  $q$  are the coefficients of the decomposition of the mass eigenstates  $|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$ . This implies that  $|A_\Gamma| < |x| \lesssim 5 \times 10^{-3}$  [6].

This Letter presents a measurement of  $A_\Gamma$  with  $pp$  collision data collected by LHCb in Run 1, corresponding to an integrated luminosity of  $3 \text{ fb}^{-1}$ , with  $1 \text{ fb}^{-1}$  collected during 2011 at a center-of-mass energy of 7 TeV and  $2 \text{ fb}^{-1}$  collected during 2012 at 8 TeV. The measurements presented are independent of the center-of-mass energy, but the two periods are analyzed separately to account for differences in cross sections and in the general running conditions. The charge of the pion from the  $D^{*+} \rightarrow D^0\pi^+$  ( $D^{*-} \rightarrow \bar{D}^0\pi^-$ ) decay is used to identify the flavor of the  $D^0$  ( $\bar{D}^0$ ) meson at production. Two different approaches are used to perform the measurement of  $A_\Gamma$ . The first is a new method based on Eq. (1) and provides the more precise results. This is described in the following text, unless otherwise stated. The other method, based on Eq. (2), has been described previously in Ref. [11] and is only summarized here. In the following, inclusion of charge-conjugate processes is implied throughout, unless otherwise stated.

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The LHCb detector [12,13] is a single-arm forward spectrometer covering the pseudorapidity range  $2 < \eta < 5$ , designed for the study of particles containing  $b$  or  $c$  quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector, surrounding the  $pp$  interaction region and allowing  $c$  hadrons to be identified by their characteristic flight distance, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm and three stations of silicon-strip detectors and straw drift tubes placed downstream of the magnet. Two ring-imaging Cherenkov detectors provide particle identification to distinguish kaons from pions. The polarity of the dipole magnet is periodically reversed during data taking. The configuration with the magnetic field vertically upwards (downwards), MagUp (MagDown), bends positively (negatively) charged particles in the horizontal plane towards the center of the Large Hadron Collider. The LHCb coordinate system is a right-handed system, with the  $z$  axis pointing along the beam direction,  $y$  pointing vertically upwards, and  $x$  pointing in the horizontal direction away from the collider center.

An online event selection is performed by a trigger system [14], consisting of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction. All events passing the hardware trigger are analyzed. Both the software trigger and the subsequent event selection use kinematic and topological variables to separate signal decays from the background. In the software trigger, two oppositely charged particles are required to form a  $D^0$  candidate that is significantly displaced from any primary  $pp$  interaction vertex (PV) in the event, and at least one of these two particles must have a minimum momentum transverse to the beam direction of 1.7 GeV/ $c$  or 1.6 GeV/ $c$ , depending on the running conditions. The  $D^0$  candidates are combined with all possible pion candidates (“soft pions”) to form  $D^{*+}$  candidates. No requirements are imposed on the soft pions at trigger level.

Offline requirements are placed on the  $D^{*+}$  vertex fit quality, where the vertex formed by the  $D^0$  and the soft  $\pi^+$  candidate is constrained to coincide with a PV, the  $D^0$  flight distance and transverse momentum, the angle between the  $D^0$  momentum and the vector from the PV to the  $D^0$  decay vertex, and the  $\chi_{\text{IP}}^2$  value of each of the  $D^0$  decay products, where  $\chi_{\text{IP}}^2$  is defined as the difference between the vertex fit  $\chi^2$  of a PV reconstructed with and without the particle under consideration. The two signal samples,  $\pi^+\pi^-$  and  $K^+K^-$ , plus the Cabibbo-favored  $K^-\pi^+$  control sample, are defined imposing further requirements on the particle identification likelihood, which is calculated from a combination of information from the Cherenkov detectors and the tracking system [15]. About 13% of the selected events have more than one candidate, mostly due to a single  $D^0$  candidate being associated with multiple soft pions. One of those candidates is then selected at random.

The  $D^0$  signal region is defined by the requirement that the invariant mass be within  $\pm 24$  MeV/ $c^2$  (approximately  $\pm 3$  times the mass resolution) of the known value [16]. The reconstructed decay times of charm mesons that originate from weak decays of  $b$  hadrons (secondary decays) are biased towards positive values, and thus, these decays are treated as background. This contamination is reduced to a few percent by requiring the reconstructed  $D^0$  momentum to point back to the PV, and  $\chi_{\text{IP}}^2(D^0) < 9$ . A systematic uncertainty on the final measurement is assigned due to the residual secondary background. The signal yields of the  $K^+K^-$ ,  $\pi^+\pi^-$  and  $K^-\pi^+$  samples, obtained by fitting the distributions of the invariant mass difference  $\Delta m \equiv m(D^0\pi^+) - m(D^0)$ , are reported in Table I. A Johnson  $S_U$  distribution [17] plus the sum of three Gaussian functions is used to model the signal, while the background is described by an empirical function of the form  $1 - \exp[(\Delta m - \Delta m_0)/\alpha] + \beta(\Delta m/\Delta m_0 - 1)$ , where  $\Delta m_0$  is the threshold of the function, and  $\alpha$  and  $\beta$  describe its shape.

The effect of a small residual background of fake  $D^{*+}$  candidates, dominated by real  $D^0$  decays associated with uncorrelated pions, is removed by a sideband-subtraction procedure. The signal region is defined as  $\Delta m \in [144.45, 146.45]$  MeV/ $c^2$ , about  $\pm 5$  times the  $\Delta m$  resolution, and the sideband region as  $\Delta m \in [149, 154]$  MeV/ $c^2$ . The uncertainty associated with this procedure is accounted for within the systematic uncertainty.

The structure of the LHCb detector is nearly symmetric under reflection in the vertical plane containing the beam axis. Nevertheless, departures from the nominal geometry and variations of the efficiency in different parts of the detector produce small residual deviations from an ideally symmetric detector acceptance. An important part of the analysis is therefore the determination and correction of these residual asymmetries. The method to achieve this is developed by exploiting the large control sample available in the  $D^0 \rightarrow K^-\pi^+$  mode, where the time-dependent asymmetry is expected to be negligible. The distribution of the  $D^0$  decay time in the range  $[0.6\tau_D, 20\tau_D]$  is divided into 30 approximately equally populated bins, and the  $D^0\text{-}\bar{D}^0$  yield asymmetry after background removal is determined in each of them. The lower bound is introduced to remove the initial turn-on region of the trigger efficiency

TABLE I. Signal yields in millions after all selection requirements.

Subsample	$D^0 \rightarrow K^-\pi^+$	$D^0 \rightarrow K^+K^-$	$D^0 \rightarrow \pi^+\pi^-$
2011 MagUp	10.7	1.2	0.4
2011 MagDown	15.5	1.7	0.5
2012 MagUp	30.0	3.3	1.0
2012 MagDown	31.3	3.4	1.1
Total	87.5	9.6	3.0

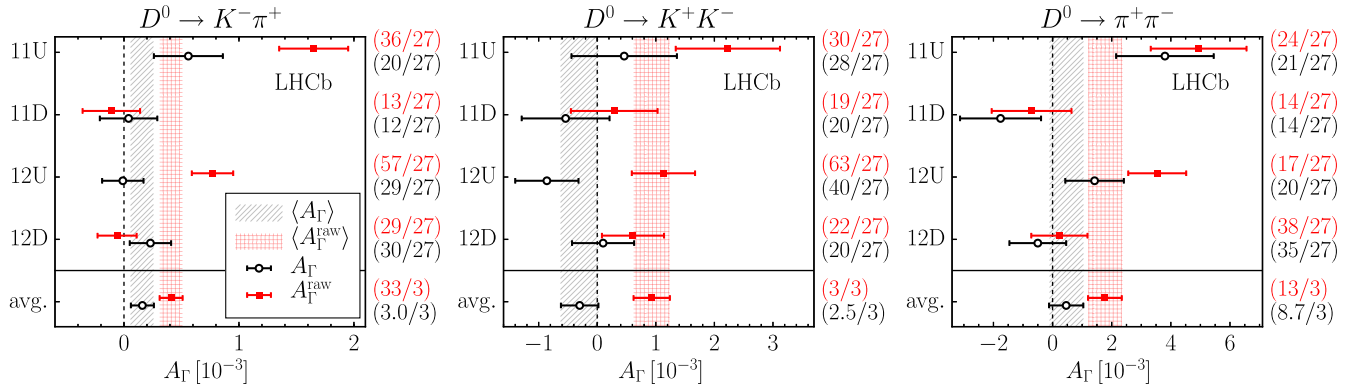


FIG. 1. Results from  $A_T$  fits in each subsample before (solid red squares) and after (empty black dots) the asymmetry correction. Fit qualities ( $\chi^2/\text{number of degrees of freedom}$ ) are also reported to the right of each graph. The weighted average of the four  $A_T$  values is indicated before (red hatched band) and after (black hatched band) the correction. The numerical values for the averages are  $A_T(K^-\pi^+) = (0.41 \pm 0.10) \times 10^{-3}$ ,  $A_T(K^+K^-) = (0.93 \pm 0.31) \times 10^{-3}$ , and  $A_T(\pi^+\pi^-) = (1.77 \pm 0.57) \times 10^{-3}$  before the correction and  $A_T(K^-\pi^+) = (0.16 \pm 0.10) \times 10^{-3}$ ,  $A_T(K^+K^-) = (-0.30 \pm 0.32) \times 10^{-3}$ , and  $A_T(\pi^+\pi^-) = (0.46 \pm 0.58) \times 10^{-3}$  after the correction. The label 2011 (2012) is abbreviated 11 (12) and MagUp (MagDown) is abbreviated  $U(D)$ .

to avoid potential biases due to charge asymmetries of the quickly varying acceptance function. The measured asymmetry  $A(t)$  is then fitted with a linear function of the decay time in units of  $\tau_D$ , the slope of which is taken as the estimate of  $A_T$  [see Eq. (1)]. For the  $\pi^+\pi^-$  and  $K^+K^-$  final states, the slope is kept blind until the completion of the analysis. The slope for the  $K^-\pi^+$  sample, expected to be unmeasurably small, is not blinded. Figure 1 shows the values of  $A_T$  obtained in the four subsamples defined in Table I. The presence of significant deviations from zero for the control channel indicates the existence of non-negligible time-dependent residual detector asymmetries. They partially cancel in the combination of the MagUp and MagDown samples but not completely, yielding an overall average that is incompatible with zero. These residual biases arise due to correlations between the decay time and other kinematic variables that affect the efficiency, most notably the momentum of the soft pion.

A correction to remove the dependence of detection asymmetries on the soft pion kinematics is applied in the time-integrated  $(k, q_s\theta_x, \theta_y)$  distribution, where  $k = 1/\sqrt{p_x^2 + p_z^2}$  is proportional to the curvature of the trajectory in the magnetic field,  $q_s$  is the sign of the soft pion charge, and  $\theta_x = \arctan(p_x/p_z)$  and  $\theta_y = \arctan(p_y/p_z)$  are the pion emission angles in the bending and vertical planes, respectively. In the absence of any asymmetry in the sample or in the detector acceptance, this distribution should be identical for  $D^{*+}$  and  $D^{*-}$  decays. A statistically significant asymmetry is, however, observed in the  $K^-\pi^+$  data (Fig. 2), where the most visible features are due to geometric boundaries of the detector, where the acceptance for positive and negative tracks differ. For each of the three decay modes, candidates are therefore weighted to fulfill  $N^+(k, +\theta_x, \theta_y) = N^-(k, -\theta_x, \theta_y)$ , where  $N^\pm$  is the number of reconstructed  $D^{*\pm}$  decays in a given bin.

The granularity of the correction is finer in  $(k, q_s\theta_x)$  than in  $\theta_y$ , where only small nonuniformities are present [18].

The weighting procedure corrects for any asymmetry of the detector response but also removes any global asymmetry caused by either  $CP$  violation or differences in the production cross sections for  $D^{*+}$  and  $D^{*-}$ . Simulation studies have confirmed that this procedure, while canceling the time-integrated asymmetry, has no significant effect on a possible genuine time-dependent asymmetry. The asymmetry correction is independently determined and applied within each subsample; the convergence of all  $A_T$  values for the  $K^-\pi^+$  control sample to a common value, as seen in Fig. 1 (top), thus provides a cross-check of the validity of the method. Independent application of the same asymmetry correction procedure to the  $D^0 \rightarrow K^+K^-$  and  $D^0 \rightarrow \pi^+\pi^-$  modes also leads to good quality for the decay-time fit in each subsample and good consistency among subsamples, as shown in Fig. 1 (bottom left and bottom right).

Another effect that needs to be accounted for in the measurement of  $A_T$  is the residual contamination from  $D^{*+}$  mesons produced in  $b$ -hadron decays. This contribution to the measured asymmetry is described with the expression

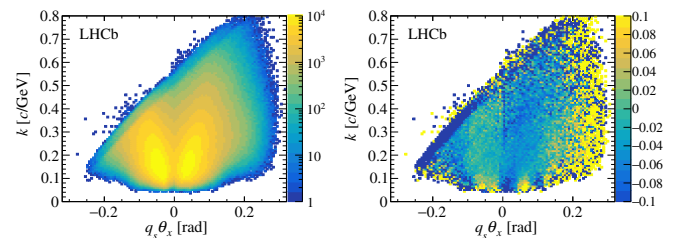


FIG. 2. (Left) Sum and (right) asymmetry of distributions of positive and negative soft pions in the  $(k, q_s\theta_x)$  plane for the 2011 MagUp  $D^0 \rightarrow K^-\pi^+$  subsample after integration over  $\theta_y$ .

$$A(t) = (1 - f_{\text{sec}}(t))A_{\text{prompt}}(t) + f_{\text{sec}}(t)A_{\text{sec}}(t),$$

where  $A_{\text{prompt}}(t)$  and  $A_{\text{sec}}(t)$  are the asymmetries for prompt and secondary components, and  $f_{\text{sec}}(t)$  is the fraction of secondary decays in the sample at decay time  $t$ . This fraction is estimated from a simulation-based model calibrated by the yield of secondary decays in data, obtained at high values of  $t$  from fits to the  $\chi_{\text{IP}}^2(D^0)$  distribution, while  $A_{\text{sec}}(t)$  is obtained from a data sample with  $\ln(\chi_{\text{IP}}^2(D^0)) > 4$ . From these estimates, the maximum effect of the contamination of secondary decays is assessed as  $\delta A_{\Gamma}^{KK} = 0.08 \times 10^{-3}$  and  $\delta A_{\Gamma}^{\pi\pi} = 0.12 \times 10^{-3}$ , accounting for the uncertainty due to the determination of  $A_{\text{sec}}(t)$  and  $f_{\text{sec}}(t)$  and for the possible contribution of nonzero values of  $A_{\Gamma}^{KK}$  and  $A_{\Gamma}^{\pi\pi}$  [18]. These effects are much smaller than the statistical uncertainties and are assigned as systematic uncertainties.

Many other effects have been examined as potential sources of systematic uncertainty. The uncertainty on the random pion background subtraction has been evaluated from the measured asymmetry of the background and its variation across the mass range surrounding the signal peak in the  $\Delta m$  distribution, yielding an uncertainty of  $\delta A_{\Gamma} = 0.01 \times 10^{-3}$  for both modes. The effect of approximating the continuous three-dimensional  $(k, q, \theta_x, \theta_y)$  asymmetry correction with a discrete function has been estimated by repeating the extraction of  $A_{\Gamma}$  in the  $K^-\pi^+$  control sample with twice or half the number of bins, which leads to an uncertainty of  $0.02 \times 10^{-3}$  for both decay modes. An additional uncertainty in the  $K^+K^-$  mode due to the presence of a peaking background from real  $D^{*+} \rightarrow D^0\pi^+$  decays, with the  $D^0$  meson decaying into other final states, has been evaluated as  $\delta A_{\Gamma}^{KK} = 0.05 \times 10^{-3}$ , based on a study of the sidebands of the  $D^0$  candidate mass distribution. Other possible sources of systematic uncertainty, including the resolution of the decay-time measurement, are found to be negligible.

The final results, obtained from the weighted average of the values separately extracted from time-dependent fits of each subsample (Fig. 1), are  $A_{\Gamma}(K^+K^-) = (-0.30 \pm 0.32 \pm 0.10) \times 10^{-3}$  and  $A_{\Gamma}(\pi^+\pi^-) = (0.46 \pm 0.58 \pm 0.12) \times 10^{-3}$ , where the first uncertainty is statistical and the second is systematic. Time-dependent asymmetries averaged over the full Run 1 data sample are compared with fit results in Fig. 3.

The complementary analysis based on Eq. (2) follows a procedure largely unchanged from the previous LHCb analysis [11], described in Refs. [19,20] and briefly summarized below. The selection requirements for this method differ from those based on Eq. (1) only in the lack of a requirement on  $\chi_{\text{IP}}^2(D^0)$ . A similar blinding procedure is used. This analysis is applied to the  $2 \text{ fb}^{-1}$  subsample of the present data, collected in 2012, that was not used in Ref. [11]. The 2012 data are split into three data-taking

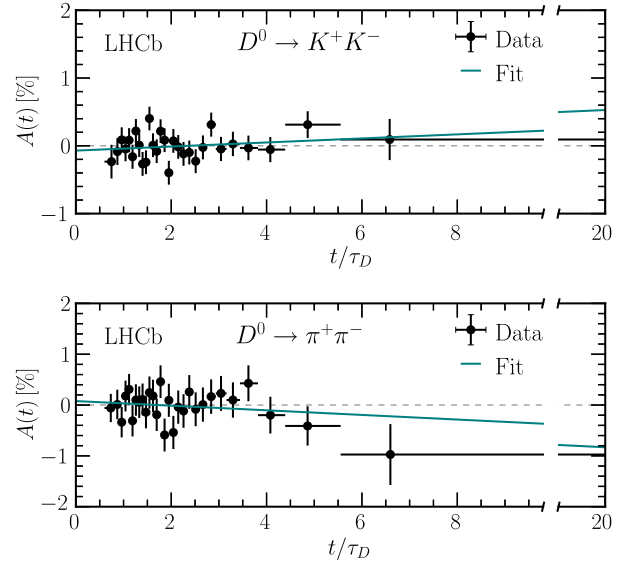


FIG. 3. Measured asymmetry  $A(t)$  in bins of  $t/\tau_D$ , where  $\tau_D = 0.410 \text{ ps}$  [16] for (top)  $D^0 \rightarrow K^+K^-$  and (bottom)  $D^0 \rightarrow \pi^+\pi^-$ , averaged over the full Run 1 data sample. Solid lines show the time dependence with a slope equal to the best estimates of  $-A_{\Gamma}$ .

periods to account for known differences in the detector alignment and calibration after detector interventions.

Biases on the decay-time distribution, introduced by the selection criteria and detection asymmetries, are accounted for through per-candidate acceptance functions, as described in Ref. [20]. These acceptance functions are parametrized by the decay-time intervals within which a candidate would pass the event selection if its decay time could be varied. They are determined using a data-driven method and used to normalize the per-candidate probability density functions over the decay-time range in which the candidate would be accepted.

A two-stage unbinned maximum likelihood fit is used to determine the effective decay widths. In the first stage, fits to the  $D^0$  mass and  $\Delta m$  spectra are used to determine yields of signal decays and both combinatorial and partially reconstructed backgrounds. In the second stage, a fit to the decay-time distribution, together with  $\ln(\chi_{\text{IP}}^2(D^0))$  (Fig. 4), is made to separate secondary background. The finding of an asymmetry consistent with zero in the control channel,  $A_{\Gamma}(K^-\pi^+) = (-0.07 \pm 0.15) \times 10^{-3}$ , validates the method. Small mismodeling effects are observed in the decay-time fits, and a corresponding systematic uncertainty of  $0.04 \times 10^{-3}$  ( $0.09 \times 10^{-3}$ ) for  $K^+K^-$  ( $\pi^+\pi^-$ ) is assigned. The largest systematic uncertainty for the  $A_{\Gamma}$  measurement, with  $K^+K^-$  ( $\pi^+\pi^-$ ), is  $0.08 \times 10^{-3}$  ( $0.10 \times 10^{-3}$ ) due to the uncertainty in modeling the contamination from the secondary (combinatorial) background. The results from the 2012 data sample are  $A_{\Gamma}(K^+K^-, 2012) = (-0.03 \pm 0.46 \pm 0.10) \times 10^{-3}$  and  $A_{\Gamma}(\pi^+\pi^-, 2012) = (0.03 \pm 0.79 \pm 0.16) \times 10^{-3}$ . These results are then combined with results from Ref. [11]

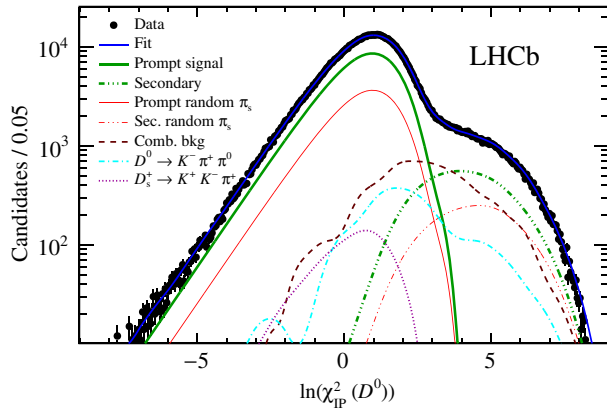


FIG. 4. Distribution of  $\ln(\chi_{\text{IP}}^2(D^0))$  for the  $D^0 \rightarrow K^+K^-$  candidates selected in the second of the three 2012 data-taking periods with magnetic field pointing downwards. The unbinned maximum likelihood fit results are overlaid. Gaussian kernels are used to smooth the combinatorial and partially reconstructed backgrounds.

to yield the final Run 1 measurements:  $A_\Gamma(K^+K^-) = (-0.14 \pm 0.37 \pm 0.10) \times 10^{-3}$  and  $A_\Gamma(\pi^+\pi^-) = (0.14 \pm 0.63 \pm 0.15) \times 10^{-3}$ .

These results can be compared with the final results from the method based on Eq. (1). An analysis has been carried out to estimate the statistical correlation between the results from the two methods, with the conclusion that they agree within one standard deviation. Because of the large correlation, the measurements from the two methods are not combined, but rather, the more precise one is chosen as the nominal result.

The results for  $D^0 \rightarrow K^+K^-$  and  $D^0 \rightarrow \pi^+\pi^-$  are consistent and show no evidence of  $CP$  violation. Assuming that only indirect  $CP$  violation contributes to  $A_\Gamma$  [5] and accounting for correlations between the systematic uncertainties [21], the two values, obtained with the method using Eq. (1), can be averaged to yield a single value of  $A_\Gamma = (-0.13 \pm 0.28 \pm 0.10) \times 10^{-3}$ , while their difference is  $\Delta A_\Gamma = (-0.76 \pm 0.66 \pm 0.04) \times 10^{-3}$ . The above average is consistent with the result obtained by LHCb in a muon-tagged sample [22], which is statistically independent. The two results are therefore combined to yield an overall LHCb Run 1 value  $A_\Gamma = (-0.29 \pm 0.28) \times 10^{-3}$  for the average of the  $K^+K^-$  and  $\pi^+\pi^-$  modes. The measurements of  $A_\Gamma$  reported in this Letter are the most precise to date and are consistent with previous results [11,23,24]. They supersede the previous LHCb measurement [11] with an improvement in precision by nearly a factor of two.

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