


Observation of a New Excited D_s^+ Meson in $B^0 \rightarrow D^- D^+ K^+ \pi^-$ DecaysR. Aaij *et al.**
(LHCb Collaboration) (Received 19 November 2020; accepted 18 February 2021; published 26 March 2021)

Using pp collision data corresponding to an integrated luminosity of 5.4 fb^{-1} collected with the LHCb detector at a center-of-mass energy of 13 TeV, the $B^0 \rightarrow D^- D^+ K^+ \pi^-$ decay is studied. A new excited D_s^+ meson is observed decaying into the $D^+ K^+ \pi^-$ final state with large statistical significance. The pole mass and width, and the spin parity of the new state are measured with an amplitude analysis to be $m_R = 2591 \pm 6 \pm 7 \text{ MeV}$, $\Gamma_R = 89 \pm 16 \pm 12 \text{ MeV}$, and $J^P = 0^-$, where the first uncertainty is statistical and the second systematic. Fit fractions for all components in the amplitude analysis are also reported. The new resonance, denoted as $D_{s0}(2590)^+$, is a strong candidate to be the $D_s(2^1S_0)^+$ state, the radial excitation of the pseudoscalar ground-state D_s^+ meson.

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Charm meson spectroscopy is of great theoretical and experimental interest as a testing ground for models based on quantum chromodynamics (QCD). In particular, the spectrum of charm-strange mesons has drawn particular attention since the discoveries of the $D_{s0}^*(2317)^+$ and $D_{s1}(2460)^+$ resonances [1,2], with masses much smaller than those predicted for $c\bar{s}$ mesons [3]. Interpretations of these states as compact $[cq][\bar{s}\bar{q}]$ tetraquarks [4,5] or $D^{(*)}K$ molecules [6,7] have been proposed. Recent evidence for exotic mesons containing cs rather than $c\bar{s}$ quarks [8,9], has raised further interest in the interpretation of the $D_{s0}^*(2317)^+$ and $D_{s1}(2460)^+$ states. Additional experimental input on the spectrum of $c\bar{s}$ mesons is essential to solve this puzzle.

Meson states are characterized by $n^{2S+1}L_J$, and grouped according to nL , where n is the principal quantum number, L is the orbital angular momentum between the constituent quarks (S, P, D correspond to $L = 0, 1, 2$), $S = 0$ or 1 is the sum of quark spins and J is the total spin of the meson. In the charm-strange meson system, candidates for the two $1S$ mesons and the four $1P$ states are experimentally well established [10]. Candidates for two of the four $1D$ states have also been reported, but their properties need further experimental confirmation [11]. Only one radial excitation, the 2^3S_1 state $D_{s1}^*(2700)^+$, is currently known. Among the missing resonances, the 2^1S_0 state, the radial excitation of the pseudoscalar ground-state D_s^+ meson, is expected to be the lightest, with mass around 2.6 GeV. Natural units with

$\hbar = c = 1$ are used, and the inclusion of charge-conjugate processes is implied throughout this Letter.

Studies of B -meson decays have proven to provide excellent potential to discover new charm-strange mesons and measure their properties [12–15]. Most such studies to date, however, only address excited D_s^+ mesons decaying into a DK pair, and hence are only sensitive to D_s^+ states with natural spin parity ($J^P = 0^+, 1^-, 2^+, \dots$) due to parity conservation in strong decays. The possibility to study production in B decays of D_s^+ resonances decaying to the $D^+ K^+ \pi^-$ final state has not been explored previously, providing opportunities to discover states with masses above 2.5 GeV. The $K^+ \pi^-$ system can be assumed to be in S wave ($J^P = 0^+$) if its mass is restricted to be below the threshold for $K^*(892)^0$ production. In this case only D_s^+ resonances with unnatural spin-parity ($J^P = 0^-, 1^+, 2^-, \dots$) can decay to $D^+ K^+ \pi^-$.

In this Letter, the observation of a new excited D_s^+ state in the $D^+ K^+ \pi^-$ mass spectrum is presented. The results are obtained from an amplitude analysis of $B^0 \rightarrow D^- D^+ K^+ \pi^-$ decays, where the $K^+ \pi^-$ mass is restricted to be lower than 0.75 GeV, referred to hereafter as the low $K^+ \pi^-$ mass region. The analysis makes use of the pp collision data collected by the LHCb experiment from 2016 to 2018 at a center-of-mass energy of 13 TeV, corresponding to an integrated luminosity of 5.4 fb^{-1} .

The LHCb detector [16,17] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The on-line event selection is performed by a trigger that consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction [18,19]. The momentum scale is calibrated using samples of $J/\psi \rightarrow \mu^+ \mu^-$ and $B^+ \rightarrow J/\psi K^+$ decays collected concurrently

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with the data sample used for this analysis [20,21]. Simulated samples are produced with the software packages described in Refs. [22–27] and are used to model the effects of the detector acceptance and the imposed selection requirements.

Signal B^0 candidates are formed using $B^0 \rightarrow D^- D^+ K^+ \pi^-$ decays with D^\pm candidates reconstructed in the $K^\mp \pi^\pm \pi^\pm$ final state. All final-state particles are required to have particle-identification information consistent with their respective mass hypotheses, and to be inconsistent with originating from any primary pp collision vertex (PV). The opening angle between any two of the final-state particles is required to be larger than 0.5 mrad to suppress potential background from repeated use of track segments. The D^\pm candidates are required to have good vertex-fit quality and mass within ± 25 MeV of the known value [10]. The decay vertex of the B^0 candidate is required to be well reconstructed, to be significantly displaced from all PVs, and to be on a trajectory consistent with having originated from the associated PV. Both D^+ and D^- vertices are required to be significantly displaced from the B^0 vertex to suppress contributions from B^0 decays involving one or no D^\pm mesons but having the same set of final tracks. A kinematic fit is applied to the decay chain to improve the B^0 mass resolution, requiring the B^0 candidate to originate from the associated PV and constraining the masses of the D^\pm candidates to their known values [10]. The B^0 -candidate mass is additionally constrained to the known value [10] in the amplitude analysis. For events with multiple B^0 candidates, only that with the lowest kinematic-fit χ^2 is retained.

Background contributions from misidentification of a final-state pion, kaon, or proton in a b -hadron decay to the $D^- D^+ h^+ h'^-$ final state with $h^{(\prime)} \in (\pi, K, p)$ are from Cabibbo-suppressed processes and thus negligible. An exception is the $B_s^0 \rightarrow D^- D^+ K^+ K^-$ decay, which instead is suppressed by the ratio of fragmentation fractions f_s/f_d [28,29] and the lack of expected contributions from any charm or charm-strange resonances. Partially reconstructed backgrounds with a missing soft neutral pion from the $D^{*+} \rightarrow D^+ \pi^0$ decay are also possible but fall below the considered B^0 -candidate mass window of ± 100 MeV around the known B^0 mass [10]. Partially reconstructed background involving $D^{*+} \rightarrow D^+ \gamma$ decay could have a tail that enters the mass window but is suppressed by its low branching fraction [10]. Hence the only significant source of background that passes the selection is due to random combinations of particles.

An unbinned maximum-likelihood fit is performed to the mass distribution of the B^0 candidates in the low $K^+ \pi^-$ mass region shown in Fig. 1. The signal is modeled by a sum of two Crystal Ball functions [30] with a common mean and opposite-side tails. The background is modeled by an exponential function. The B^0 signal yield is

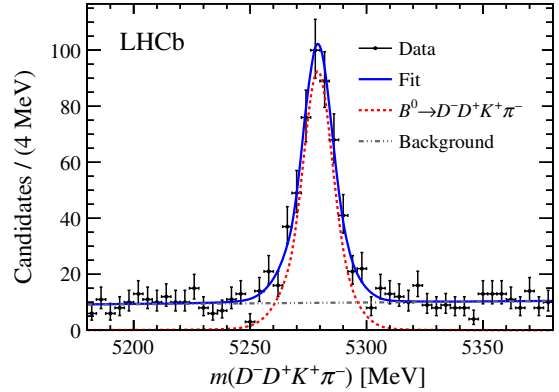


FIG. 1. Mass distribution of the selected B^0 candidates in the low $K^+ \pi^-$ mass region. The fit result is overlaid.

determined to be 444 ± 27 , where the uncertainty is statistical. The Dalitz plot [31] of the $D^+ D^-$ versus $D^+ K^+ \pi^-$ masses-squared for candidates with masses within 20 MeV of the known B^0 mass [10] is shown in Fig. 2. A clear cluster of candidates is observed in the $D^+ K^+ \pi^-$ mass at $\sqrt{6.8 \text{ GeV}^2} \approx 2.6$ GeV. No $D^+ D^-$ resonant structure is apparent. The $D^+ K^+ \pi^-$ mass projection is shown in Fig. 3(a), where a structure at about 2.6 GeV, which has never been observed before, is evident and the small peak just above threshold corresponds to the $D_{s1}(2536)^+$ state [32].

An amplitude analysis is employed to study structures in the $D^+ K^+ \pi^-$ system of B^0 candidates in the low $K^+ \pi^-$ mass region. Three D_s^+ components with unnatural spin parity are considered: a new D_s^+ state at about 2.6 GeV denoted hereafter as D_{sJ}^+ due to its undetermined spin parity, the $J^P = 1^+$ $D_{s1}(2536)^+$ state, and a $J^P = 0^-$ nonresonant (NR) component. The line shape of the $K^+ \pi^-$ system is modeled by the $J^P = 0^+$ $K_0^*(700)^0$ state

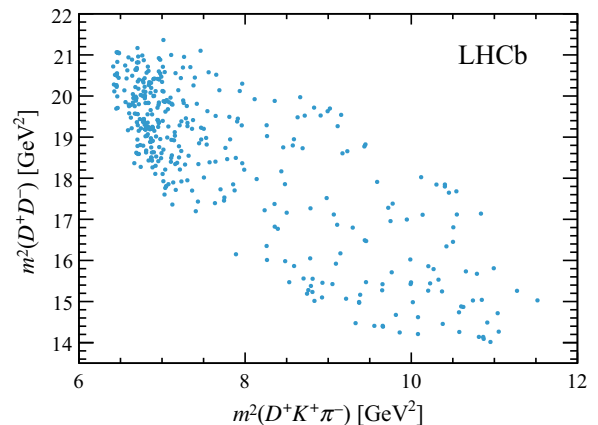


FIG. 2. Dalitz plot of the $D^+ D^-$ versus $D^+ K^+ \pi^-$ masses squared for B^0 candidates with masses within ± 20 MeV around the known B^0 mass [10] in the low $K^+ \pi^-$ mass region.

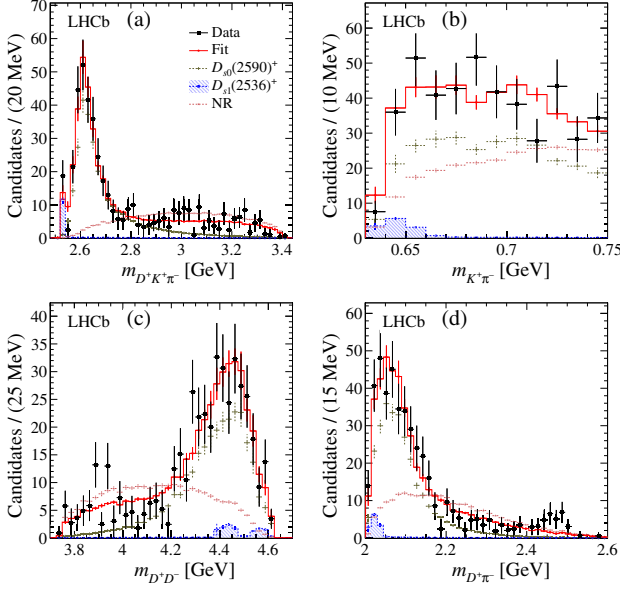


FIG. 3. Mass projections of (a) $D^+K^+\pi^-$, (b) $K^+\pi^-$, (c) D^+D^- , and (d) $D^+\pi^-$ systems. Data points are shown in black with the background subtracted statistically using the *sPlot* method [33]. Results of the fit with the $D_{s0}(2590)^+$ ($J^P = 0^-$) model are overlaid as a solid red histogram, and individual contributions shown as dotted histograms.

for all three D_s^+ components. The amplitude is constructed using the helicity formalism [34], with the total amplitude given by

$$\mathcal{M} = \sum_k \mathcal{H}^{D_{sk}} d_{0,0}^{J_{D_{sk}}}(\theta_{D_s}) p^{L_{B^0}} F_{L_{B^0}}(pa) q^{L_{D_{sk}}} F_{L_{D_{sk}}}(qa) \times \text{BW}(m_{K^+\pi^-}) \text{BW}_{D_{sk}}(m_{D^+K^+\pi^-}),$$

where the summation is over the three D_s^+ components. Here $\mathcal{H}^{D_{sk}}$ is the complex helicity coupling parameter describing the magnitude and the phase of the D_{sk} component, and $d_{0,0}^{J_{D_{sk}}}(\theta_{D_s})$ is the Wigner small- d matrix with the two subscripts set to zero and the superscript corresponding to the spin of the D_{sk} component, where θ_{D_s} is the angle between the directions of D^+ momentum and the opposite of the B^0 momentum, both in the D_s^+ rest frame. The quantity $p(q)$ is the momentum of the decay products of the B^0 (D_{sk}) state in its rest frame, and $L_{B^0}(L_{D_{sk}})$ is the orbital angular momentum between the decay products of the B^0 (D_{sk}) state. The function $F_L(z)$ is the Blatt-Weisskopf form factor that accounts for the barrier of the decay [35–37], in which $z \equiv pa$ or qa and the parameter a describes the size of the decaying particle, set to $3 \text{ GeV}^{-1} \sim 0.6 \text{ fm}$. The line shapes of the D_{sJ}^+ , $D_{s1}(2536)^+$, and $K_0^*(700)^0$ states are described by relativistic Breit-Wigner (BW) functions. The NR component has a constant line shape.

Different expressions for the width $\Gamma(m)$ that enters the BW function are used for the D_{sJ}^+ , $D_{s1}(2536)^+$ and $K_0^*(700)^0$ states. The $D_{s1}(2536)^+$ width is set to constant as it is very narrow, while a two-body mass-dependent width is used for the $K_0^*(700)^0$ state; in both cases the BW parameters are fixed to their known values [10,38]. The total D_{sJ}^+ width is described as the sum of contributions from the open decay channels to two-body D^*K and three-body $DK\pi$ decays,

$$\Gamma^{D_{sJ}^+}(m_{D^+K^+\pi^-}) = \Gamma^{D_{sJ}^+ \rightarrow D^*K}(m_{D^+K^+\pi^-}) + \Gamma^{D_{sJ}^+ \rightarrow DK\pi}(m_{D^+K^+\pi^-}),$$

where $\Gamma^{D_{sJ}^+ \rightarrow D^*K}$ and $\Gamma^{D_{sJ}^+ \rightarrow DK\pi}$ are the partial widths for the corresponding decays. The former is parameterized with a two-body mass-dependent width and the latter is set to a constant.

The signal model in the amplitude analysis is the amplitude squared $|\mathcal{M}|^2$ multiplied by an efficiency function and normalized to unity when integrated over the phase space. The unknown parameters of the signal model, denoted hereafter as $\vec{\omega}$, are the complex helicity coupling parameters of the D_{sJ}^+ and $D_{s1}(2536)^+$ states, the BW mass and width of the D_{sJ}^+ state, and the width fraction of the $D_{sJ}^+ \rightarrow D^*K$ channel defined as $r = \Gamma^{D_{sJ}^+ \rightarrow DK\pi}(m_0) / \Gamma^{D_{sJ}^+}(m_0)$, where m_0 is the BW mass. The helicity coupling parameter of the NR component is fixed to unity to serve as a reference amplitude. The optimal values of the parameters, $\vec{\omega}_{\text{min}}$, are determined with the same method used, and described in detail in Ref. [39]. An unbinned fit minimizes the negative log-likelihood, $-2 \ln \mathcal{L}(\vec{\omega})$, with the background subtracted statistically using weights obtained with the *sPlot* method with the B^0 -candidate mass as the discriminating variable. The variables in the amplitude analysis, $m_{D^+K^+\pi^-}$, $m_{K^+\pi^-}$ and θ_{D_s} , are confirmed not to have strong correlations with the B^0 -candidate mass, as required in the *sPlot* method. The non-parametric efficiency function is determined from simulation with corrections applied to ensure the trigger efficiency, B^0 kinematics and track multiplicity match those observed in data.

Three possible spin-parity models of the D_{sJ}^+ state are tested: $J^P = 0^-$, 1^+ , and 2^- , among which the $J^P = 0^-$ model leads to the best fit quality. This is understood by the property of $d_{0,0}^J(\theta_{D_s})$ describing the $\cos \theta_{D_s}$ behavior of the D_{sJ}^+ state in the amplitude, which is proportional to the Legendre polynomial of order J and is squared in the signal model. Thus, the $\cos \theta_{D_s}$ distribution is described by a constant function for $J^P = 0^-$, a second-order polynomial for $J^P = 1^+$ and a fourth-order polynomial for $J^P = 2^-$. The $J^P = 0^-$ model is clearly seen to be most consistent with data, as shown in Fig. 4.

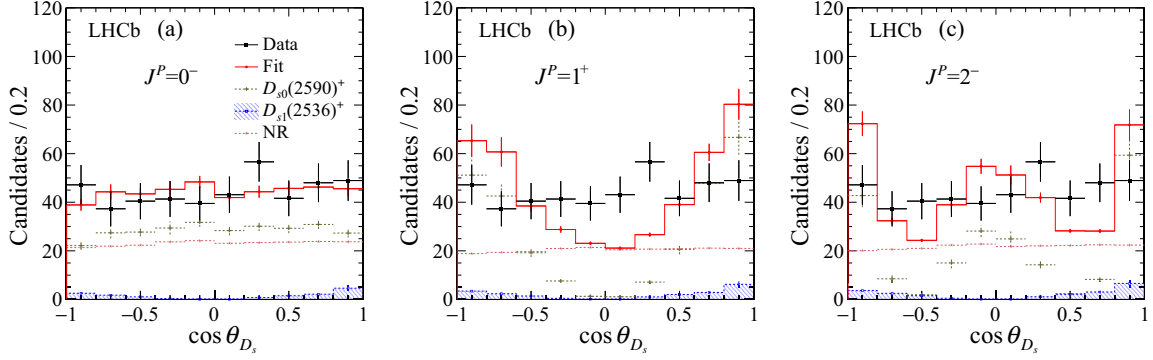


FIG. 4. Comparison of $\cos \theta_{D_s}$ distributions for the spin parity of the $D_{s0}(2590)^+$ state assumed to be (a) 0^- , (b) 1^+ , and (c) 2^- . The $J^P = 0^-$ model is the most consistent with data. Data points are shown in black with the background subtracted statistically using the *sPlot* method [33]. Fit results are overlaid as a solid red histogram, with individual contributions shown as dotted histograms.

The significance to reject each of the disfavored spin-parity models and the model without the D_{sJ}^+ state is evaluated using the method of Refs. [39,40]. The difference of $-2 \ln \mathcal{L}(\tilde{\omega}_{\min})$ between two models is assumed to follow a χ^2 distribution. The number of degrees of freedom associated with this χ^2 distribution is 1 when comparing two models with different spin-parity hypotheses, and twice the difference in the number of freely varying parameters when comparing models with different numbers of components. Taking the $J^P = 0^-$ model as the reference, models without the D_{sJ}^+ state or with $J^P = 1^+$ or 2^- are all rejected with significance over 10 standard deviations. Therefore, the spin parity of the D_{sJ}^+ state is determined to be $J^P = 0^-$. The D_{sJ}^+ state is hereafter denoted as $D_{s0}(2590)^+$.

Almost equally good fit quality and the same $D^+ K^+ \pi^-$ mass line shape are found for different width fractions r in the range 0 to 1, indicating that this parameter cannot be determined using the current data. The value of r is fixed to 0.5. The fitted BW mass and width of the $D_{s0}(2590)^+$ state vary significantly for different width fractions, but its pole position $m_R - i\Gamma_R/2$, where m_R and Γ_R are the pole mass and width, is found to be stable. This is understood as a consequence of the BW parameters being dependent on specific reactions and width parameterizations, and as such having no strict physical meaning. In contrast, the pole position is independent of the reaction studied and the chosen width parameterization, and is a physical characteristic of a resonance [10]. Therefore, only the pole mass and width of the $D_{s0}(2590)^+$ state are reported in this Letter. These are measured to be $m_R = 2591 \pm 6$ and $\Gamma_R = 89 \pm 16$ MeV, where the uncertainty is statistical. Several mass projections are shown in Fig. 3. The enhancements in data at high $m_{D^+D^-}$ and low $m_{D^+\pi^-}$ are seen to be well described as reflections of the $D_{s0}(2590)^+$ contribution. A small excess is seen in $m_{D^+\pi^-}$ near the mass of the $D_2^*(2460)^0$ state, which populates the region higher than 3 GeV in $m_{D^+K^+\pi^-}$, far away from the $D_{s0}(2590)^+$ peak.

Therefore, vetoing it has small impact on the measured properties and is taken into account as a source of systematic uncertainty. Mass distributions of combinations of final-state particles not shown in Fig. 3 do not exhibit any structures.

Fit fractions, defined as in Ref. [9], for the three D_s^+ components in the low $K^+\pi^-$ mass region obtained from the fit are listed in Table I. The interference fraction between the $D_{s0}(2590)^+$ and NR components is also listed, whose negative central value explains why the full amplitude distribution lies below the NR distribution in some regions, as shown in Fig. 3. The ratio of the $D_{s1}(2536)^+$ and $D_{s0}(2590)^+$ fit fractions is also given in Table I.

Systematic uncertainties on the measured properties are summarized in Table II. The primary source is related to the choice of the $D_{s0}(2590)^+$ width model, which is evaluated by describing the partial width of the $D_{s0}(2590)^+ \rightarrow DK\pi$ channel with a three-body formula similar to that used in Ref. [41], instead of constant, or varying the width fraction r between 0 and 1. Other sources include variation of the $D_{s1}(2536)^+$ mass shape due to uncertainties in the BW parameters and the width model, as well as the effect of detector resolution [which, at $\mathcal{O}(1$ MeV), is negligible for

TABLE I. Fit fractions for the three D_s^+ components in the low $K^+\pi^-$ mass region ($m_{K^+\pi^-} < 0.75$ GeV). The interference fraction between the $D_{s0}(2590)^+$ and NR components is denoted as $D_{s0}^+ \text{-NR}$. There is no net interference between any other pair of components due to the orthogonality of the Wigner small- d matrices for different spins. D_{s1}^+/D_{s0}^+ denotes the ratio of the $D_{s1}(2536)^+$ and $D_{s0}(2590)^+$ fit fractions.

	Fit fraction ($\times 10^{-2}$)
$D_{s0}(2590)^+$	$63 \pm 9(\text{stat}) \pm 9(\text{syst})$
$D_{s1}(2536)^+$	$3.9 \pm 1.4(\text{stat}) \pm 0.8(\text{syst})$
NR	$51 \pm 11(\text{stat}) \pm 19(\text{syst})$
$D_{s0}^+ \text{-NR}$	$-18 \pm 18(\text{stat}) \pm 24(\text{syst})$
D_{s1}^+/D_{s0}^+	$6.1 \pm 2.4(\text{stat}) \pm 1.4(\text{syst})$

TABLE II. Systematic uncertainties on the pole mass and width of the $D_{s0}(2590)^+$ state, and fit fractions of the three D_s^+ components. The individual sources are added in quadrature to obtain the total uncertainty. The notations are the same as these in Table I.

Source	m_R [MeV]	Γ_R [MeV]	Fit fraction ($\times 10^{-2}$)				
			D_{s0}^+	D_{s1}^+	NR	$D_{s0}^+-\text{NR}$	D_{s1}^+/D_{s0}^+
$D_{s0}(2590)^+$ width model	6.1	8.0	4.7	0.0	15.0	19.6	0.5
$D_{s1}(2536)^+$ mass shape	0.3	4.3	2.3	0.6	3.5	5.3	1.1
$K^+\pi^-$ mass shape	2.7	2.6	3.0	0.2	1.2	4.4	0.1
Blatt-Weisskopf factor	0.7	3.4	2.8	0.3	1.3	3.0	0.2
Including $c\bar{c}$ resonances	1.1	5.4	2.7	0.1	6.3	10.0	0.4
$D^+\pi^-$ resonance veto	2.4	2.1	4.6	0.3	9.4	4.6	0.2
Simulation correction	0.2	1.1	0.3	0.1	0.7	0.8	0.2
Momentum calibration	0.5	0.4	1.3	0.0	1.4	2.5	0.2
Total	7.2	11.7	8.6	0.8	19.3	23.9	1.4

broader structures]; the description of the $K^+\pi^-$ mass shape evaluated by using the LASS model [42] and by varying within uncertainties the BW parameters of the $K_0^*(700)^0$ state; variation of the Blatt-Weisskopf barrier factor, R , between 1.5 and 4.5 GeV^{-1} ; inclusion of possible $c\bar{c}$ resonances, such as $\psi(3770)$, $\chi_{c0}(3930)$, and $\chi_{c2}(3930)$; vetoing possible $D^+\pi^-$ resonant contributions by requiring $m_{D^+\pi^-} < 2.4$ GeV; imperfections in the corrections applied to simulated events; and imperfect momentum calibration due to limited knowledge of the magnetic field and the detector alignment. Uncertainties related to the size of the simulation sample are negligible. The total systematic uncertainty is obtained by combining all contributions in quadrature.

In conclusion, a new excited D_s^+ meson is observed with large statistical significance in the $D^+K^+\pi^-$ system of $B^0 \rightarrow D^-D^+K^+\pi^-$ decays. The analysis makes use of pp collision data collected by the LHCb experiment, corresponding to an integrated luminosity of 5.4 fb^{-1} . An amplitude analysis is performed on data in the low $K^+\pi^-$ mass region, $m_{K^+\pi^-} < 0.75$ GeV, and the pole mass and width, and the spin parity of the new state are measured to be $m_R = 2591 \pm 6 \pm 7$ MeV, $\Gamma_R = 89 \pm 16 \pm 12$ MeV, and $J^P = 0^-$, where the first uncertainty is statistical and the second systematic. Fit fractions obtained in the amplitude analysis are also reported. The new resonance, denoted as $D_{s0}(2590)^+$, is a strong candidate to be the missing $D_s(2^1S_0)^+$ state, the radial excitation of the pseudoscalar ground-state D_s^+ meson.

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- [1] B. Aubert *et al.* (BABAR Collaboration), Observation of a Narrow Meson Decaying to $D_s^+\pi^0$ at a Mass of $2.32 \text{ GeV}/c^2$, *Phys. Rev. Lett.* **90**, 242001 (2003).
- [2] D. Besson *et al.* (CLEO Collaboration), Observation of a narrow resonance of mass $2.46 \text{ GeV}/c^2$ decaying to $D_s^{*+}\pi^0$ and confirmation of the $D_{sJ}^*(2317)$ state, *Phys. Rev. D* **68**, 032002 (2003); Erratum, *Phys. Rev. D* **75**, 119908 (2007).
- [3] S. Godfrey and K. Moats, Properties of excited charm and charm-strange mesons, *Phys. Rev. D* **93**, 034035 (2016).
- [4] L. Maiani, F. Piccinini, A. D. Polosa, and V. Riquer, Diquark-antidiquark states with hidden or open charm and the nature of $X(3872)$, *Phys. Rev. D* **71**, 014028 (2005).
- [5] T. E. Browder, S. Pakvasa, and A. A. Petrov, Comment on the new $D_s^{(*)+}\pi^0$ resonances, *Phys. Lett. B* **578**, 365 (2004).
- [6] T. Barnes, F. E. Close, and H. J. Lipkin, Implications of a DK molecule at 2.32 GeV , *Phys. Rev. D* **68**, 054006 (2003).

- [7] E. van Beveren and G. Rupp, Observed $D_s(2317)$ and Tentative $D(2100-2300)$ as the Charmed Cousins of the Light Scalar Nonet, *Phys. Rev. Lett.* **91**, 012003 (2003).
- [8] R. Aaij *et al.* (LHCb Collaboration), Model-Independent Study of Structure in $B^+ \rightarrow D^+D^-K^+$ Decays, *Phys. Rev. Lett.* **125**, 242001 (2020).
- [9] R. Aaij *et al.* (LHCb Collaboration), Amplitude analysis of the $B^+ \rightarrow D^+D^-K^+$ decay, *Phys. Rev. D* **102**, 112003 (2020).
- [10] P. A. Zyla *et al.* (Particle Data Group), Review of particle physics, *Prog. Theor. Exp. Phys.* **2020**, 083C01 (2020).
- [11] A. Palano, Experimental status of excited D_s^+ mesons, [arXiv:2009.07126](https://arxiv.org/abs/2009.07126).
- [12] J. Brodzicka *et al.* (Belle Collaboration), Observation of a New D_{sJ} Meson in $B^+ \rightarrow \bar{D}^0D^0K^+$ Decays, *Phys. Rev. Lett.* **100**, 092001 (2008).
- [13] J. P. Lees *et al.* (BABAR Collaboration), Dalitz plot analyses of $B^0 \rightarrow D^-D^0K^+$ and $B^+ \rightarrow \bar{D}^0D^0K^+$ decays, *Phys. Rev. D* **91**, 052002 (2015).
- [14] R. Aaij *et al.* (LHCb Collaboration), Observation of Overlapping Spin-1 and Spin-3 \bar{D}^0K^- Resonances at Mass $2.86 \text{ GeV}/c^2$, *Phys. Rev. Lett.* **113**, 162001 (2014).
- [15] R. Aaij *et al.* (LHCb Collaboration), Dalitz plot analysis of $B_s^0 \rightarrow \bar{D}^0K^-\pi^+$ decays, *Phys. Rev. D* **90**, 072003 (2014).
- [16] A. A. Alves, Jr. *et al.* (LHCb Collaboration), The LHCb detector at the LHC, *J. Instrum.* **3**, S08005 (2008).
- [17] R. Aaij *et al.* (LHCb Collaboration), LHCb detector performance, *Int. J. Mod. Phys. A* **30**, 1530022 (2015).
- [18] R. Aaij *et al.*, The LHCb trigger and its performance in 2011, *J. Instrum.* **8**, P04022 (2013).
- [19] T. Likhomanenko, P. Iiten, E. Khairullin, A. Rogozhnikov, A. Ustyuzhanin, and M. Williams, LHCb topological trigger reoptimization, *J. Phys. Conf. Ser.* **664**, 082025 (2015).
- [20] R. Aaij *et al.* (LHCb Collaboration), Measurements of the Λ_b^0 , Ξ_b^- , and Ω_b^- Baryon Masses, *Phys. Rev. Lett.* **110**, 182001 (2013).
- [21] R. Aaij *et al.* (LHCb Collaboration), Precision measurement of D meson mass differences, *J. High Energy Phys.* **06** (2013) 065.
- [22] T. Sjöstrand, S. Mrenna, and P. Skands, A brief introduction to PYTHIA 8.1, *Comput. Phys. Commun.* **178**, 852 (2008).
- [23] I. Belyaev *et al.*, Handling of the generation of primary events in Gauss, the LHCb simulation framework, *J. Phys. Conf. Ser.* **331**, 032047 (2011).
- [24] D. J. Lange, The EvtGen particle decay simulation package, *Nucl. Instrum. Methods Phys. Res., Sect. A* **462**, 152 (2001).
- [25] P. Golonka and Z. Was, PHOTOS Monte Carlo: A precision tool for QED corrections in Z and W decays, *Eur. Phys. J. C* **45**, 97 (2006).
- [26] J. Allison *et al.* (Geant4 Collaboration), Geant4 developments and applications, *IEEE Trans. Nucl. Sci.* **53**, 270 (2006).
- [27] M. Clemencic, G. Corti, S. Easo, C. R. Jones, S. Miglioranza, M. Pappagallo, and P. Robbe, The LHCb simulation application, Gauss: Design, evolution and experience, *J. Phys. Conf. Ser.* **331**, 032023 (2011).
- [28] R. Aaij *et al.* (LHCb Collaboration), Measurement of b -hadron fractions in 13 TeV $p p$ collisions, *Phys. Rev. D* **100**, 031102(R) (2019).
- [29] R. Aaij *et al.* (LHCb Collaboration), Measurement of f_s/f_u Variation with Proton-Proton Collision Energy and B -Meson Kinematics, *Phys. Rev. Lett.* **124**, 122002 (2020).
- [30] T. Skwarnicki, A study of the radiative cascade transitions between the Upsilon-prime and Upsilon resonances, Ph.D. thesis, Institute of Nuclear Physics, 1986, DESY-F31-86-02.
- [31] R. H. Dalitz, On the analysis of τ -meson data and the nature of the τ -meson, *Philos. Mag. Ser. 7* **44**, 1068 (1953); E. Fabri, A study of τ -meson decay, *Nuovo Cimento* **11**, 479 (1954).
- [32] V. Balagura *et al.* (Belle Collaboration), Observation of $D_{s1}(2536)^+ \rightarrow D^+\pi^-K^+$ and angular decomposition of $D_{s1}(2536)^+ \rightarrow D^{*+}K_S^0$, *Phys. Rev. D* **77**, 032001 (2008).
- [33] M. Pivk and F. R. Le Diberder, sPlot: A statistical tool to unfold data distributions, *Nucl. Instrum. Methods Phys. Res., Sect. A* **555**, 356 (2005).
- [34] S. U. Chung, Spin formalisms, CERN Report No. CERN-71-08, 1971; J. D. Richman, An experimenter's guide to the helicity formalism, CERN Report No. CALT-68-1148, 1984; M. Jacob and G. C. Wick, On the general theory of collisions for particles with spin, *Ann. Phys. (N.Y.)* **7**, 404 (1959).
- [35] J. M. Blatt and V. F. Weisskopf, *Theoretical Nuclear Physics* (Springer, New York, 1952).
- [36] F. Von Hippel and C. Quigg, Centrifugal-barrier effects in resonance partial decay widths, shapes, and production amplitudes, *Phys. Rev. D* **5**, 624 (1972).
- [37] S. U. Chung, J. Brose, R. Hackmann, E. Klempt, S. Spanier, and C. Strassburger, Partial wave analysis in K matrix formalism, *Ann. Phys. (N.Y.)* **507**, 404 (1995).
- [38] J. P. Lees *et al.* (BABAR Collaboration), Measurement of the mass and width of the $D_{s1}(2536)^+$ meson, *Phys. Rev. D* **83**, 072003 (2011).
- [39] R. Aaij *et al.* (LHCb Collaboration), Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi p K^-$ Decays, *Phys. Rev. Lett.* **115**, 072001 (2015).
- [40] R. Aaij *et al.* (LHCb Collaboration), Amplitude analysis of $B^+ \rightarrow J/\psi \phi K^+$ decays, *Phys. Rev. D* **95**, 012002 (2017).
- [41] R. Aaij *et al.* (LHCb Collaboration), Observation of a new baryon state in the $\Lambda_b^0 \pi^+ \pi^-$ mass spectrum, *J. High Energy Phys.* **06** (2020) 136.
- [42] D. Aston *et al.*, A study of $K^+ \pi^-$ scattering in the reaction $K^+ p \rightarrow K^- \pi^+ n$ at 11 GeV/c, *Nucl. Phys.* **B296**, 493 (1988).

R. Aaij,³¹ C. Abellán Beteta,⁴⁹ T. Ackernley,⁵⁹ B. Adeva,⁴⁵ M. Adinolfi,⁵³ H. Afsharnia,⁹ C. A. Aidala,⁸⁴ S. Aiola,²⁵ Z. Ajaltouni,⁹ S. Akar,⁶⁴ J. Albrecht,¹⁴ F. Alessio,⁴⁷ M. Alexander,⁵⁸ A. Alfonso Albero,⁴⁴ Z. Aliouche,⁶¹ G. Alkhazov,³⁷

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